# Analysis of surface X-ray scattering from synthetic quartz mirror 

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## Introduction

It is important to evaluate the nm-scale structure of large-area engineering surfaces, especially when these are prepared for optical applications [1]. Surface X-ray scattering is an extremely promising method for this purpose $[2,3]$. The present report describes the quantitative determination of the surface morphologies for synthetic quartz mirror with different finishes.

## Experimental

Measured samples are synthetic quartz mirror ( 25 mmx 25 mmx 5 mm ) with optically flat surfaces of different quality, "20-2" (certified flatness $\lambda / 20$, $\lambda=632.8 \mathrm{~nm})$, " $10-5$ " $(\lambda / 10)$, "4-5" $(\lambda / 4)$ and " $1-3$ " $(\lambda)$, which are commercially available from SIGMA KOKI Co., Ltd. X-ray scattering measurements were carried out with 16.0 keV X-rays. The beam size was $0.05 \times 1.0 \mathrm{~mm}$.

## Results and Discussion

Fig. 1 shows experimental results of specular and nonspecular scattering for samples, "20-2" and " $1-3$ ". The maximum reflectivity below the critical angle, around 1.9 mrad, was $93.6 \%$ and $81.8 \%$, respectively. No oscillating structures were observed in the whole specular reflectivity curve, indicating that significant surface layers do not exist. Non-specular scattering, as shown in the inset, exhibits Yoneda peaks at around 1.8 mrad and 15.7 mrad . Those features of the data were more or less common for all the samples.

During previous studies [3], it was found that the intensity ratio of the specular and non-specular scattering is strongly correlated to the surface morphology. In the present case, the intensity at Yoneda peak ( 1.8 mrad ) is $20.5 \%, 14.2 \%, 15.2 \%$, and $11.8 \%$ to the specular scattering at 8.75 mrad , for " $1-3$ ", " $4-5$ ", " $10-5$ " and " 20 2 ", respectively. One can see that the order agrees well with that of flatness as certified by the laser-light method.

The data were analyzed based on the self-affine surface model [2], of which the height-to-height correlation function for the distance $\rho$ is given as $\mathrm{C}(\rho)=\sigma^{2} \exp [-$ $\left.(\rho / \xi)^{2 h}\right]$, where $\sigma, \xi$ and $h$ are the surface roughness, the correlation length in horizontal directions, and Hurst parameter, respectively. In the present study, simultaneous fitting has been attempted for specular and

Table 1 Summary of the curve fitting.

|  | Hurst <br> Parameter | Correlation <br> Length <br> $[\mathrm{nm}]$ | Roughness <br> $[\mathrm{nm}]$ | Density <br> Factor |
| ---: | ---: | :--- | ---: | ---: |
| $1-3$ | 0.135 | 132 | 1.36 | 1.025 |
| $4-5$ | 0.215 | 190 | 1.27 | 1.013 |
| $10-5$ | 0.235 | 263 | 1.30 | 1.048 |
| $20-2$ | 0.203 | 320 | 1.28 | 1.006 |

non-specular (rocking and detector scans) data. The results are summarized in Table 1. The rms roughness $\sigma$ was different, but quite close for the four samples, around 1.3 nm . This is not so surprising considering that their specular reflectivity did not show such big differences even in the higher-angle region ( $7 \sim 14 \mathrm{mrad}$ ). On the other hand, $\xi$ and $h$ are quite different. One can see that density factor also exhibits differences. It has been found that "20-2" is quite normal and has a moderate surface, while " $1-3$ " has an extraordinarily jagged surface. The authors would like to thank Prof. S. Kishimoto for his assistance during the experiment.

## References

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Fig. 1 Experimental results of specular and non-specular (inset, rocking scan at 17.5 mrad fixed scattering angle) reflections for the samples, 20-2 and 1-3. Fitted curves are shown as solid lines. For the rocking scan, the calculation only considers the non-specular portion, while the experimental data include specular reflection.

