

Anomalous Scattering Factor near Absorption Edge of Ge

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The measured anomalous scattering factor (ASF, $f + if''$) near Ge K absorption edge traces a circular arc as shown in Fig.1¹⁾. According to the quantum theory of X-ray resonant scattering, ASF can be given by the following equation in case of only one resonant mode,²⁾

$$f + if'' \propto -1 / (\Delta\omega + i\Gamma/2) \quad (1)$$

Where, $\Delta\omega = \omega_n - \omega$ ω_n is resonant energy and Γ is the natural width of spectrum. The circle-like locus of $f + if''$ in Fig.1 can be obtained by changing $\Delta\omega$. If the energy of the initial peak just above the edge in f'' curve in Fig.2 is assigned to be ω_M and its height $\Delta f''_M$ after subtracting the background to be the diameter of the circle in Fig.1, the following equation can be derived from equation (1)

$$\Delta f + i\Delta f'' = -\Delta f''_M / (x + i) \quad (2)$$

Where $x = 2(\omega_M - \omega) / \Gamma$ and $\omega_M = \omega_K + \Gamma/2$. Equation (2) is rewritten as

$$\Delta f = -x \Delta f''_M / (x^2 + 1), \quad \Delta f'' = \Delta f''_M / (x^2 + 1). \quad (3a,b)$$

In order to get the ASF ($f'_C + if''_C$) in a real crystal, it is necessary to add $\Delta f + \Delta f''$ to the values calculated by the isolated atom model (IAM). That is

$$f'_C = \Delta f + f'_{\text{atom}}, f''_C = \Delta f'' + f''_{\text{atom}} \quad (4a,b)$$

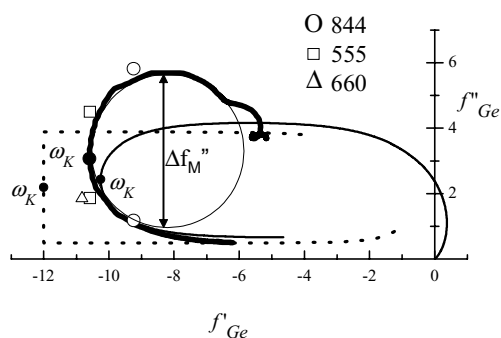


Fig.1 The Locus of the ASF in Ge. O □ Δ (zero crossing method) and thick solid line (dispersion relation) are measured values. The dashed line and solid line are calculated values of the IAM with CLS³⁾ and PH⁴⁾.

Here f'_{atom} and f''_{atom} are the real and imaginary parts of ASF given by the IAM. In the ASF of Ge crystal, $\Delta f''_M$ is determined to be 5.38 and $\Gamma/2$ is evaluated to be 2.5 ± 0.5 eV. This value is five times larger than the calculated value (0.5 eV) by using classical damping. From this result, the lifetime ($\tau = h / 2\pi\Gamma$) of the intermediate state is estimated to be 0.13 ± 0.03 fs. Then f'_C and f''_C (thick solid line) are obtained and shown in Fig.2. The ASFs determined by zero crossing method, the dispersion relation method (solid line) and the IAM³⁾ (dashed line) are shown in Fig.2. It is clear that the values of f'_C obtained by the present method are in good agreement with the zero crossing method and the dispersion method.

- 1) M. Yoshizawa *et al.*, (2003), KEK Prog. Rep. **2002-2**, 155.
- 2) T. Fukamachi and S. Hosoya (1975) Acta Cryst. **A31**, 215-220.
- 3) S. Sasaki, (1989) KEK Rep. **88-14 M/D**, 1-136.
- 4) L. G. Parratt & C. F. Hempstead, (1954) Phys. Rev. **94**, 1593-1600.

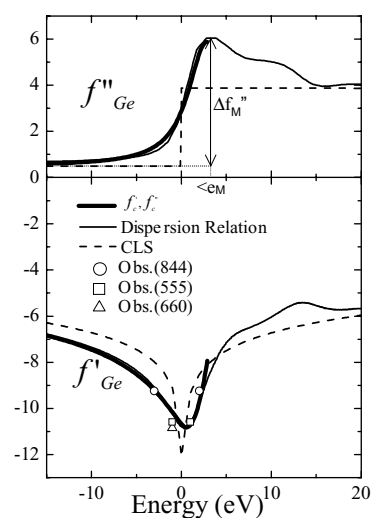


Fig. 2 The measured and the calculated ASF.

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