

# ポジトロニウム負イオン光脱離断面積の計算 (Calculation of the photo-detachment cross sections of $\text{Ps}^-$ )

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## 概要 (outline)

### 1. 理論 (Theory)

- 1.1 1光子及び2光子吸収により光脱離  
(One- and two-photo detachment)
- 1.2 原子軌道緊密結合法  
(Atomic orbital close coupling method)

### 2. 結果 (Results)

- 2.1 One-photon detachment cross section
- 2.2 Two-photon detachment cross section

# One- and two-photon detachment cross sections within the perturbation theory

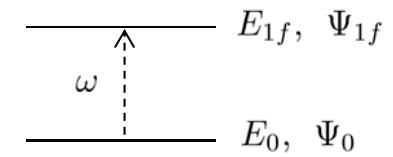
$$\sigma^{(1)} = \pi(2\pi\alpha)\omega <\Psi_{1f}|\hat{\mathbf{e}} \cdot \mathbf{D}|\Psi_0>|^2.$$

$\alpha$ : fine-structure constant.  $\omega$ : photon energy.

$\Psi_0$ : the initial bound state,  $E_0$ .

$\Psi_{1f}$ : a final scattering state,  $E_{1f} = E_0 + \omega$ .

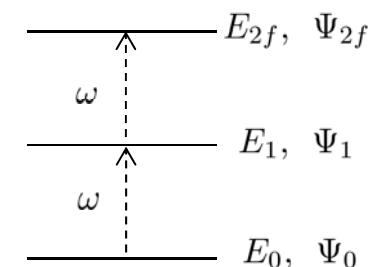
$\hat{\mathbf{e}}$ : (linear) polarization,  $\mathbf{D}$ :dipole operator.



$$\sigma^{(2)} = \pi(2\pi\alpha)^2\omega^2|A^{(2)}|^2,$$

$$A^{(2)} = \lim_{\eta \rightarrow +0} <\Psi_{2f}|\hat{\mathbf{e}} \cdot \mathbf{D} \frac{1}{E_1 - H + i\eta} \hat{\mathbf{e}} \cdot \mathbf{D}|\Psi_0>  
= <\Psi_{2f}|\hat{\mathbf{e}} \cdot \mathbf{D}|\Psi_1>$$

$$(E_1 - H)\Psi_1 = \hat{\mathbf{e}} \cdot \mathbf{D}\Psi_0, \quad E_1 = E_0 + \omega  
(E_2 - H)\Psi_{2f} = 0, \quad E_{2f} = E_0 + 2\omega$$



Ps<sup>-</sup> system (e<sup>-</sup>, e<sup>-</sup>, e<sup>+</sup>)

Kinetic energy term

$$T = -\frac{1}{2M} \nabla_{R_1}^2 - \frac{1}{2m} \nabla_{r_1}^2 = -\frac{1}{2M} \nabla_{R_2}^2 - \frac{1}{2m} \nabla_{r_2}^2$$

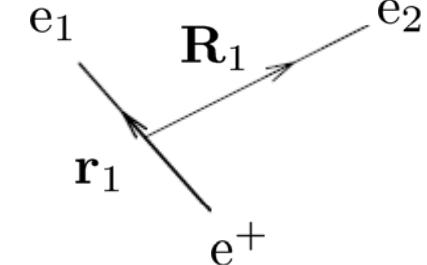
$$= -\frac{1}{2m} \nabla_{r_1}^2 - \frac{1}{2m} \nabla_{r_2}^2 - \frac{1}{m_+} \nabla_{r_1} \cdot \nabla_{r_2}$$

$$M = \frac{m_e(m_e + m_+)}{2m_e + m_+} = \frac{2}{3}m_e, \quad m = \frac{m_e m_+}{m_e + m_+} = \frac{1}{2}m_e$$

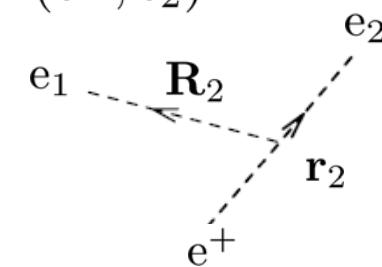
$m_e$ : electron mass,  $m_+$ : positron mass

Hamiltonian  $H = T - \frac{1}{r_1} - \frac{1}{r_2} + \frac{1}{r_{12}}$

(e<sub>1</sub>, e<sup>+</sup>) + e<sub>2</sub>



e<sub>1</sub> + (e<sup>+</sup>, e<sub>2</sub>)



Symmetry  $\Gamma = \{L, S, \Pi\}$ ,  $[H, \mathbf{L}^2] = [H, L_z] = [H, \mathbf{S}^2] = [H, \Pi] = 0$

Angular momentum  $\mathbf{L} = \mathbf{l}_{r_1} + \mathbf{l}_{r_2} = \mathbf{l}_{R_c} + \mathbf{l}_{r_c}$

Spin  $\mathbf{S} = \mathbf{s}_1 + \mathbf{s}_2$ ,

Parity,  $\Pi\psi(\mathbf{r}_1, \mathbf{r}_2) = \psi(-\mathbf{r}_1, -\mathbf{r}_2)$

Atomic orbital (AO) basis

$$\phi_{n\ell}^{\Gamma}(\mathbf{r}, \hat{\mathbf{R}}) = \frac{u_{n\ell}(r)}{r} (Y_{\ell}(\hat{\mathbf{r}}) \otimes Y_l(\hat{\mathbf{R}}))_{LM_M}$$

AO expansion,

$$\Psi^{\Gamma} = \sum_{\mu=1}^N \left( \frac{f_{\mu}(R_1)}{R_1} \phi_{\mu}^{\Gamma}(\mathbf{r}_1, \hat{\mathbf{R}}_1) + (-1)^S \frac{f_{\mu}(R_2)}{R_2} \phi_{\mu}^{\Gamma}(\mathbf{r}_2, \hat{\mathbf{R}}_2) \right)$$

$f_{\mu}$ : unknown function

From  $\int d\hat{\mathbf{R}}_1 \int d\mathbf{r}_1 \phi_{\mu}^{\Gamma*}(\mathbf{r}_1, \hat{\mathbf{R}}_1)(H - E)\Psi^{\Gamma} = 0$ ,

$$-\frac{1}{2M} \left[ \frac{d^2}{dR_1^2} - \frac{l_{\mu}(l_{\mu}+1)}{R_1^2} - k_{\mu}^2 \right] f_{\mu}(R_1) + \sum_{\nu=1}^N (V_{\mu\nu}^D + (-1)^S V_{\mu\nu}^X) f_{\nu}(R_1) = 0$$

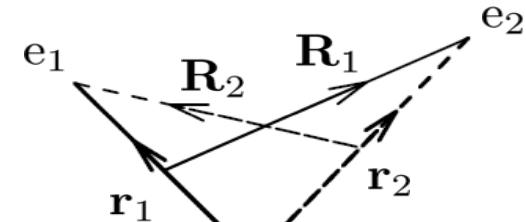
coupled integro-differential equations

$$f_{\mu}(R) = \sum_{i=1}^{N_B} C_{\mu i} B_i(R), \quad 0 \leq R \leq R_{max}, \quad C_{\mu i}: \text{coefficient}$$

$$\Psi^{\Gamma} = \sum_{i=1}^{N_B} \sum_{\mu=1}^N C_i^{\mu} \underbrace{\left( B_i(R_1) \phi_{\mu}(\mathbf{r}_1, \hat{\mathbf{R}}_1) + (-1)^S B_i(R_2) \phi_{\mu}(\mathbf{r}_2, \hat{\mathbf{R}}_2) \right)}_{\mathcal{B}_{i\mu}} \equiv \sum_{i=1}^{N_B} \sum_{\mu=1}^N C_i^{\mu} \mathcal{B}_{i\mu}$$

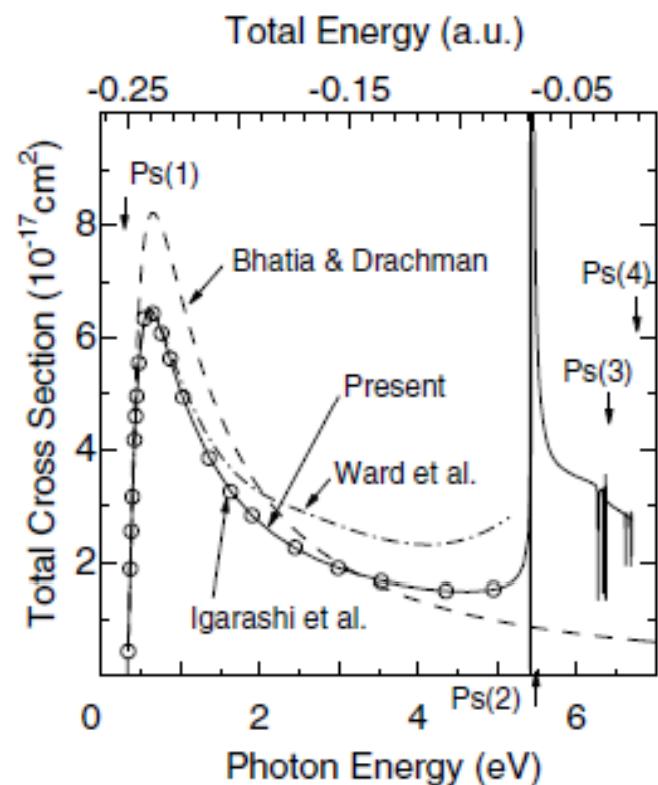
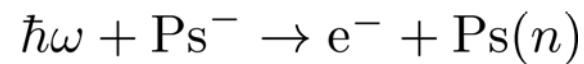
$$\int_0^{R_{max}} d\mathbf{R}_1 \int d\mathbf{r}_1 \mathcal{B}_{i\mu}^*(H - E)\Psi^{\Gamma} = 0 \rightarrow \sum_{j=1}^{N_B} \sum_{\nu=1}^N \left( \int_0^{R_{max}} d\mathbf{R}_1 \int d\mathbf{r}_1 \mathcal{B}_{i\mu}^* (H - E) \mathcal{B}_{j\nu} \right) C_j^{\nu} = 0$$

coupled integro-differential equations  $\Rightarrow$  algebraic equations

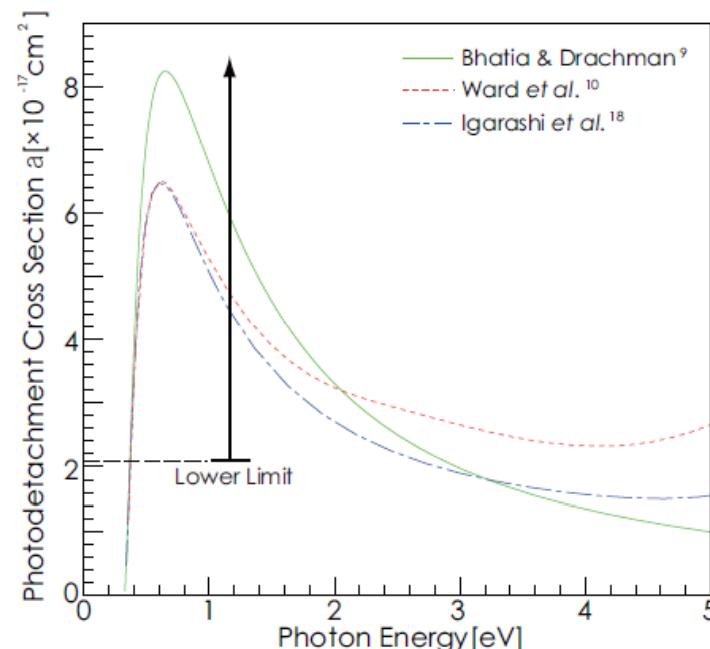


$e^+$

# One-photon detachment cross sections of $\text{Ps}^-$

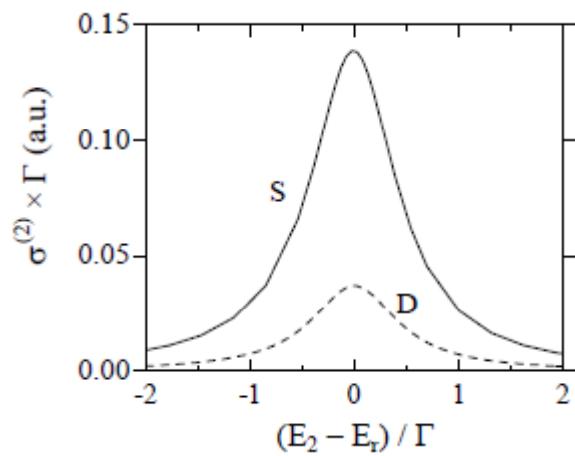
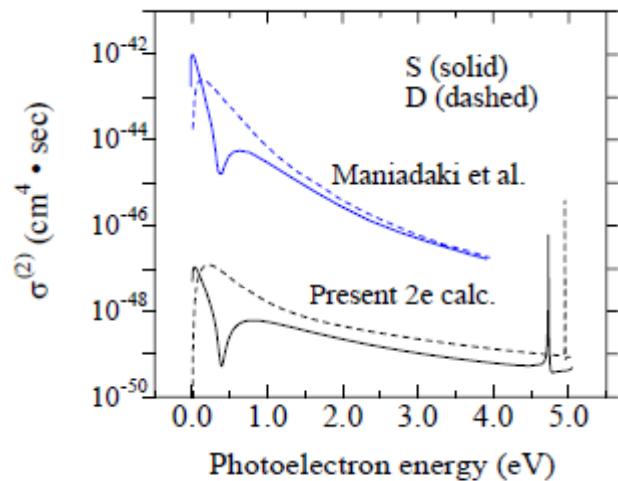


Igarashi, Shimamura, Toshima  
N. J. Phys. **2** 17 (2000)

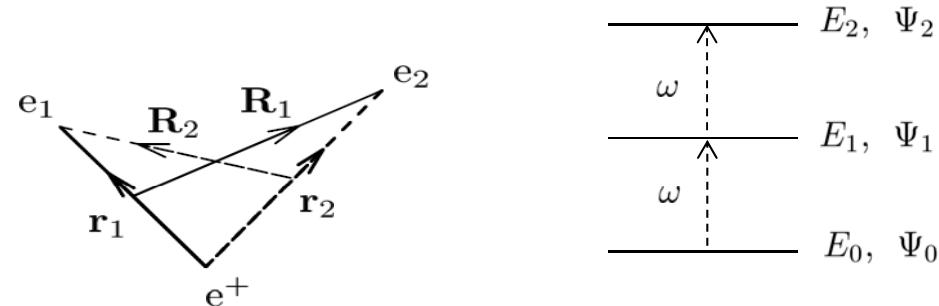


Michishio et al.  
Phys. Rev. Lett. **106**, 153401 (2011)

## Two-photon detachment cross sections of $\text{Ps}^-$



Selection rule



Resonance parameter

	$E_r$ (eV)	$\Gamma$ (meV)	
$^1\text{S}^e$	4.7340	1.2	present
	4.7340	1.2	CR
$^1\text{D}^e$	4.9550	0.050	present
	4.9549	0.049	CR

$E_r$  in photoelectron energy

- For photon energy above the one-photon detachment, one- and two photodetachments occur simultaneously.
- The best way to distinguish them is to measure the momentum of ejected electrons. But it may be difficult for  $\text{Ps}^-$  system.

Rates for one- and two-photon detachment of  $\text{Ps}^-$

Laser intensity  $I$  ( $\text{W}/\text{cm}^2$ )

$$I = \hbar\omega F,$$

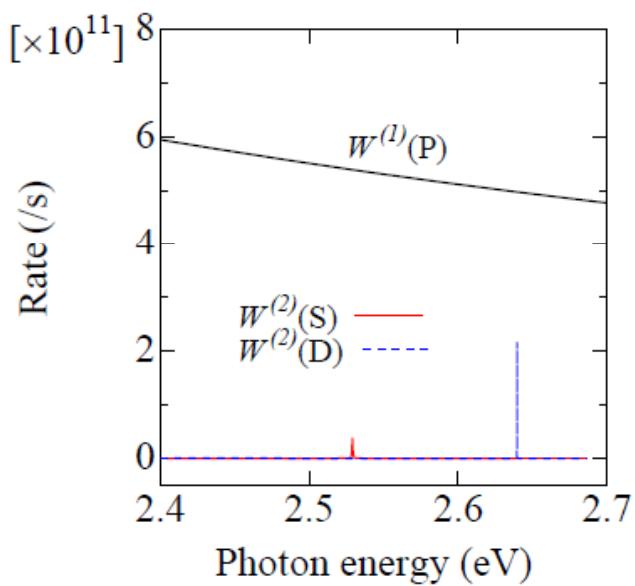
photon flux  $F$  ( $\text{photons}/(\text{cm}^2 \text{ s})$  )

Rate (/s)

$$W^{(1)} = \sigma^{(1)} F$$

$$W^{(2)} = \sigma^{(2)} F^2$$

Laser intensity  $I = 1.0 \times 10^{10} \text{ W}/\text{cm}^2$



## Summary

- Two-photon detachment cross sections ( $\sigma^{(2)}$ ) of  $\text{Ps}^-$  are calculated with the coupled channel calculations.
- The lowest  $^1\text{S}^e$  and  $^1\text{D}^e$  resonances below the  $\text{Ps}(n=2)$  threshold are clearly seen.
- To observe the resonances without measuring the ejected electron kinetic energy, the laser intensity  $\sim 1.0 \times 10^{10} \text{ W/cm}^2$  is required.