


Studies on surface systems by using electron spectroscopy with synchrotron radiation and positron diffraction

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Physical properties at a surface

- Surface atomic structure
  - Diffraction: 陽電子回折 Positron Diffraction
- Surface electronic structure
  - Spectroscopy: 光電子分光 Photoemission spectroscopy

- Mystery of the 2-D ordered metal alloy on a surface
- Introduction of our time-resolved photoemission station at synchrotron radiation facility

合金 (Metal Alloy)

**Hume-Rothery phase**  
Chapter 21, C. Kittel, "Introduction to Solid State Physics", (1996)

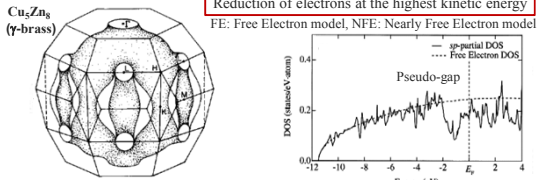
electron/atom ratio of electron compounds				
Alloys	fcc	bcc	γ	hcp
Cu-Zn	1.38	1.48	1.58-1.66	1.78-1.87
Cu-Al	1.41	1.48	1.63-1.77	
Cu-Si	1.42	1.49		
Ag-Cd	1.42	1.50	1.59-1.63	1.65-1.82

A close relation between the Fermi surface and the Brillouin zone (electron/atom) (the crystal structure)

Two competing theoretical model  
Jones theory vs Pseudopotential approach (Pair potential interpretation)

- Jones theory for alloying

Reduction of electrons at the highest kinetic energy  
FE: Free Electron model, NFE: Nearly Free Electron model



合金 (Metal Alloy)

Pair potential interpretation (long-range interaction mediated by conduction electrons)

$$E(k) = \frac{\hbar^2 k^2}{2m} + \langle k | w | k \rangle + \sum_q \frac{S^*(q)S(q) \langle k | w | k+q \rangle \langle k+q | w | k \rangle}{\hbar^2 / 2m [k^2 - (k+q)^2]}$$

Band structure energy  $E_{bs} = \sum S(q)^* S(q) F(q)$

$$E_{bs} = \frac{1}{2N} \sum_{i,j} V_{pair}(r_i - r_j) + \frac{1}{N} \sum_q F(q)$$

Ion-pair potential (structure dependent)

$$V_{pair}(r_i - r_j) = \frac{2}{N} \sum_{l,j} F(q) \exp(-iq \cdot (r_i - r_j)) \quad V_{3D} \propto \frac{\sin(2k_F d + 2\delta_F)}{(k_F d)^3}$$

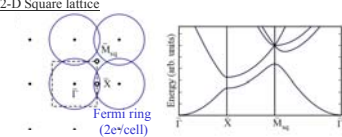
Ion pair-interaction via the 3-D Friedel oscillation

Motivation

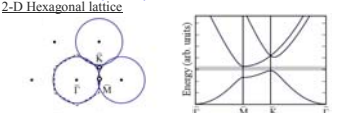
合金 (Metal Alloy)  
Formation of metal alloys of the electron compounds

表面合金 (Surface Metal Alloy)  
Any metallic surface superstructure with electron compound nature?

2-D Square lattice



2-D Hexagonal lattice

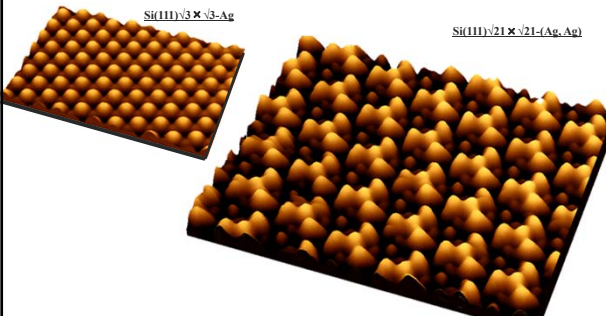


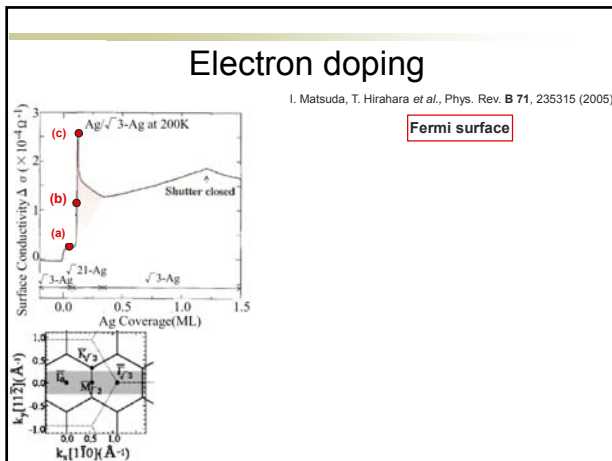
Fermi wavenumber, Fermi surface  
Crystal structure  
In-plane Fermi wavenumber, 2-D Fermi surface  
Surface ordered phase

2e/cell => Metallic  
2e/cell => Insulating => Complete gap-opening => Not pseudo-gap!!

Surface Metal Alloy (2-D Metal Alloy) on Semiconductor Substrate

Ag: 1ML (470-870K) → Si(111)√3 × √3-Ag → Ad: 0.1-0.2ML (< 200-300 K) → Si(111)√21 × √21-(Ag, Ad)





### Surface Metal Alloy (2-D Metal Alloy) on Semiconductor Substrate

The  $\sqrt{21} \times \sqrt{21}$  phase on Si(111)

Initial surface phase (coverage)	adatom (coverage)	formation temperature	total coverage	a number of valence electrons
<b>2-D surface phase</b>				
$\sqrt{3} \times \sqrt{3}$ -Ag (1.0 ML)	Au (0.1-0.2 ML)	LT	1.1-1.2 ML	3/unit cell [1]
$\sqrt{3} \times \sqrt{3}$ -Ag (1.0 ML)	Ag (0.1-0.2 ML)	LT	1.1-1.2	3 [2]
$\sqrt{3} \times \sqrt{3}$ -Ag (1.0 ML)	Na (0.1-0.2 ML)	LT	1.1-1.2	3 [2]
$\sqrt{3} \times \sqrt{3}$ -Ag (1.0 ML)	K (0.1-0.2 ML)	LT	1.1-1.2	3 [3]
$\sqrt{3} \times \sqrt{3}$ -Ag (1.0 ML)	Cs (0.1-0.2 ML)	LT	1.1-1.2	3 [3]
$\sqrt{3} \times \sqrt{3}$ -Au (-0.9 ML)	Ag (0.2-0.3 ML)	HT	1.1-1.2	3 [4]
<b>1-D surface phase</b>				
5x2-Au (0.4-0.5 ML)	Ag (-0.7 ML)	HT	1.1-1.2	3 [5]
3x1-Ag (0.3 ML)	Au (0.8 ML)	HT	1.1-1.2	3 [6]

Photoemission Fermi surface of a  $\sqrt{21} \times \sqrt{21}$

Free electron surface (long)

Extended Zone

$\sqrt{21} \times \sqrt{21}$  SBZ

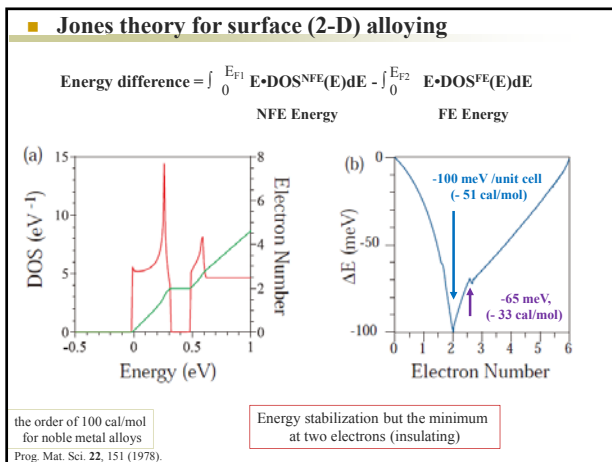
1<sup>st</sup> SBZ

2<sup>nd</sup> SBZ

3<sup>rd</sup> SBZ

The crystal phase has the constant electron/atom ratio → electron compound nature

[1] J. N. Crain et al., Phys. Rev. B 66, 205302(2002). [2] I. Matsuda et al., Phys. Rev. B 71, 235315 (2005). [3] H. M. Zhang et al., Phys. Rev. Lett. 85, 1331 (2000). [4] Y. Yuhara et al., Surf. Sci. 326, 133 (1995). [5] I. Matsuda et al., Phys. Rev. B 70, 245301 (2004). [6] F. Nakamura et al., submitted.



### Pair potential interpretation

Ion pair-interaction via the 2-D Friedel oscillation

band structure energy:  $\Delta E = \sum_{\text{ionpairs}} -\epsilon_F \left( \frac{2 \sin(\delta_F)}{\pi} \right)^2 \frac{\sin(2k_F d - 2\delta_F)}{(k_F d)^2}$

$k_F$

n=1 :  $k_F=0.153[\text{\AA}^{-1}]$   
 n=2 :  $k_F=0.216[\text{\AA}^{-1}]$   
 n=3 :  $k_F=0.265[\text{\AA}^{-1}]$   
 n: electrons/unit cell

Photoemission Fermi surface mapping

$d(d')$

Structure analysis

Distance between two adatoms (up to the 11<sup>th</sup> nearest neighbors)

### Structure analysis of the $\sqrt{21} \times \sqrt{21}$ phase

Si(111)  $\sqrt{7} \times \sqrt{7}$  Ag: 1ML 470-870K → Si(111)  $\sqrt{3} \times \sqrt{3}$ -Ag Ag: 0.1-0.2ML LT → Si(111)  $\sqrt{21} \times \sqrt{21}$ -Ag, Ag

J. Nogami et al., SS 306 (1994) 81. A. Ichimiya et al., SRL1(1994) 1

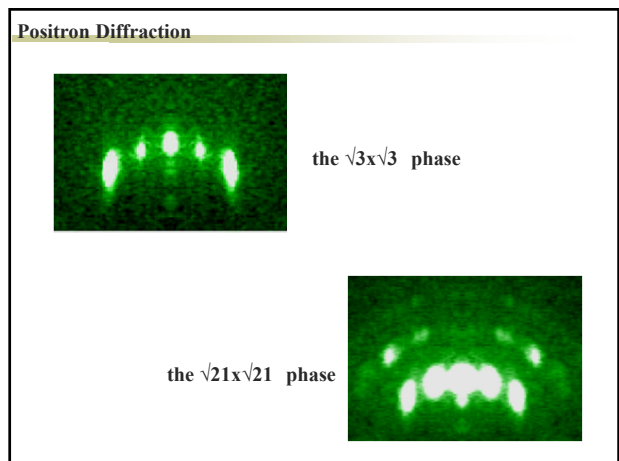
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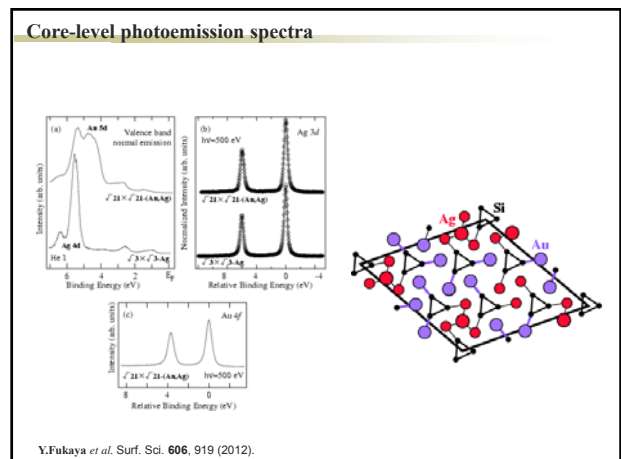
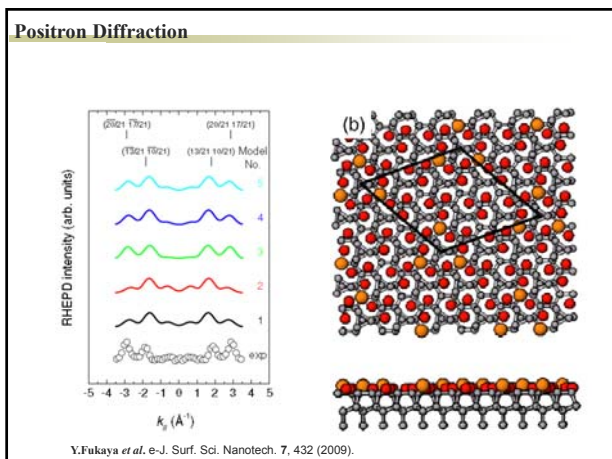
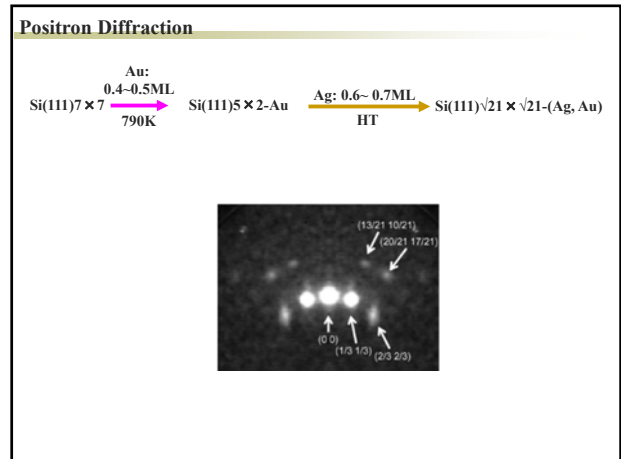
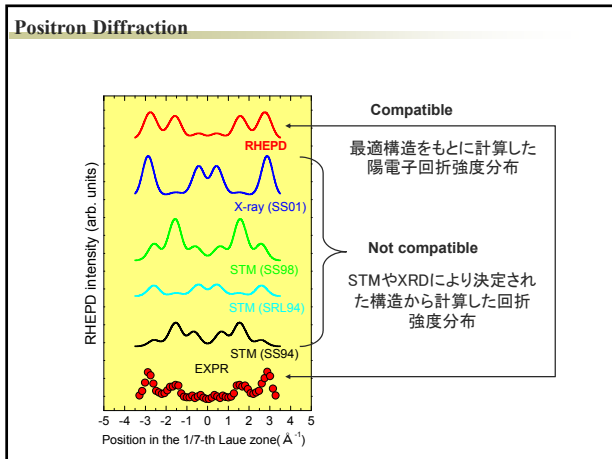
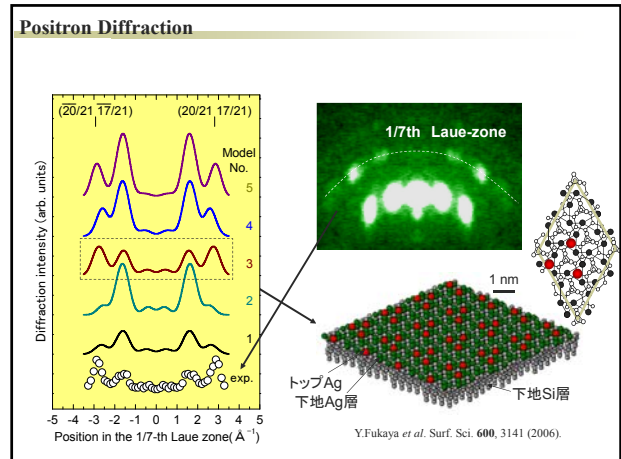
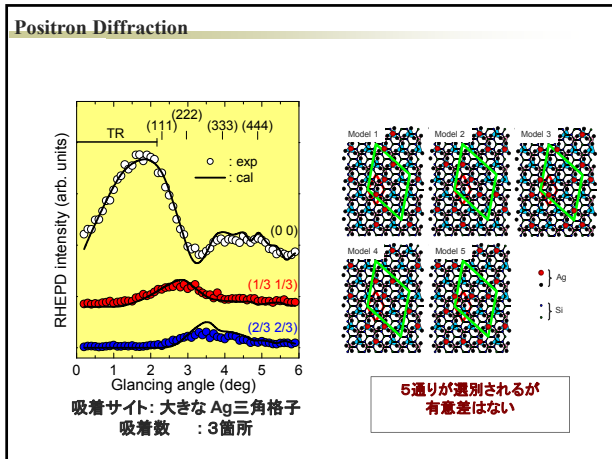
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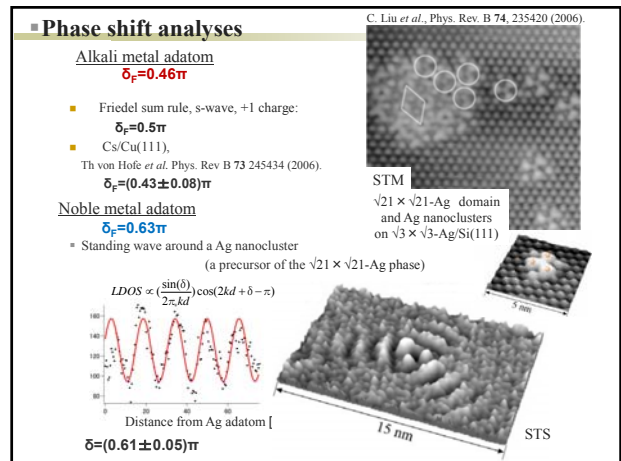
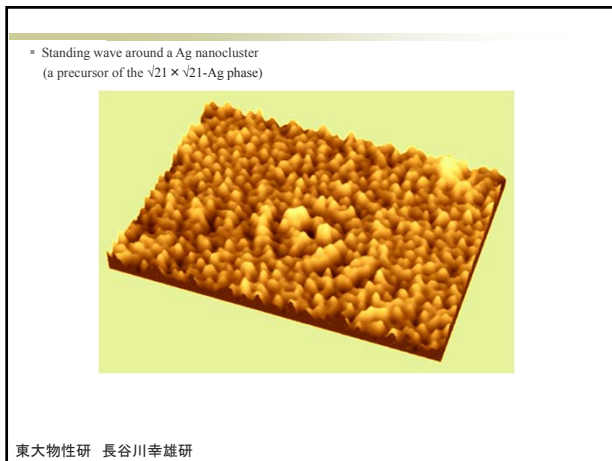
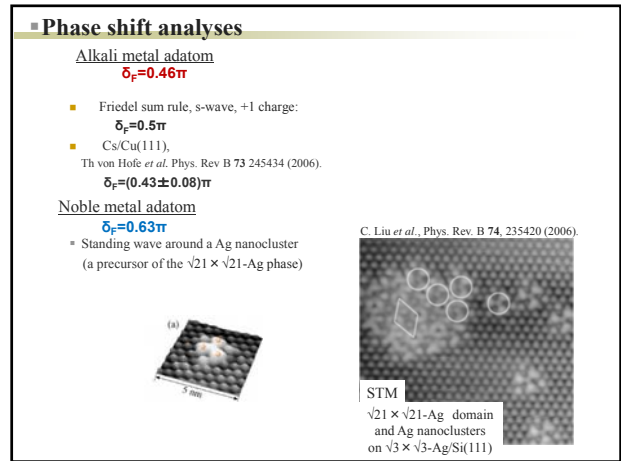
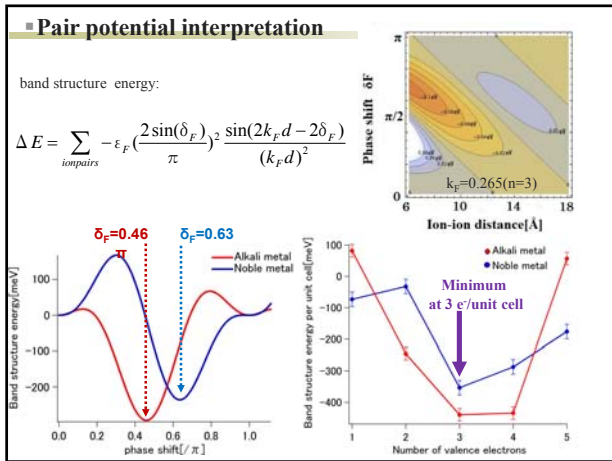
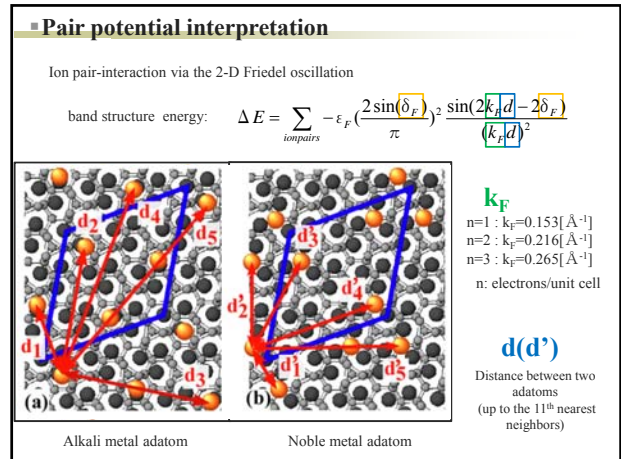
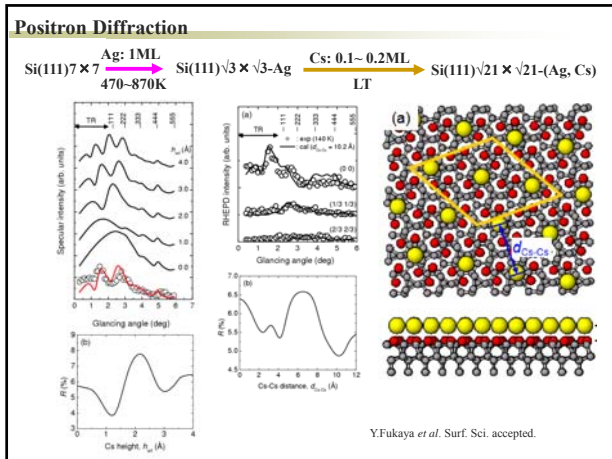
吸着可能位置数: 21箇所  
 吸着原子数 : 3-5個

${}_{21}C_3=1330$ 通り  
 ${}_{21}C_4=3990$ 通り  
 ${}_{21}C_5=20349$ 通り

X. Tong et al., PRB55(1997)1310. H. Tajiri et al., SS493(2001)214



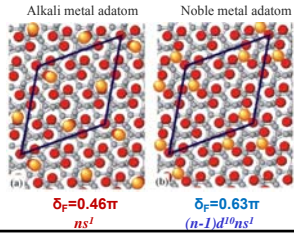
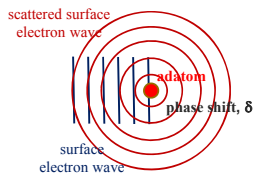




I. Matsuda *et al.*, Phys. Rev. B **82**, 165330 (2010).

- The  $\sqrt{21} \times \sqrt{21}$  phases, prepared by **eight** different procedures, show the constant number of total metal coverage and a number of valence electron, showing surface electron compound nature.
- The Anderson's idea and the Jones model do find electron stability by the surface superstructure formation. However, they fails to explain a number of valence electrons and the experimental band feature.
- The pair potential interpretation (the pseudopotential approach) explains all the experimental results, indicating importance of medium-range interatomic interaction, mediated by the 2-D surface-state electrons.

**The  $\sqrt{21} \times \sqrt{21}$  superstructure model**



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Y. Fukaya, A. Kawasuso, and A. Ichimiya

