

テラヘルツ時間領域分光法と 基礎科学への応用

Department of Physics, Kyoto University
Koichiro Tanaka

SCOPE project
2003-2007



Advanced Terahertz Technologies
adapted for **Optical Communication**



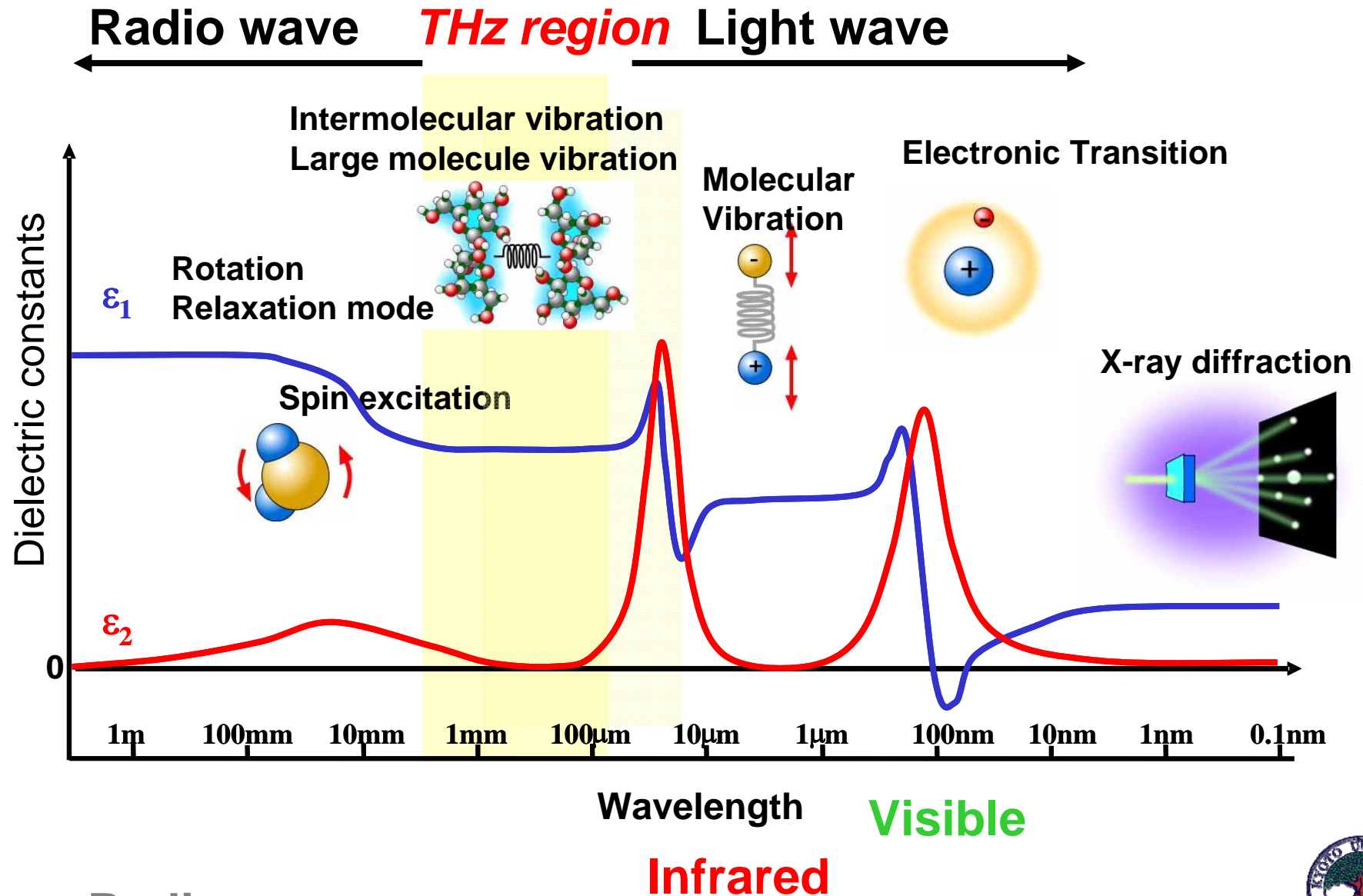
JSPS project
2006-2010

Exploitation of Organic Electronic Materials
of Potential Dynamic Switches for Non-
equilibrium Condensed Matter Sciences

講演内容

- **テラヘルツテクノロジーとは何か？**
- **時間領域テラヘルツ分光法の基礎**
- **時間領域テラヘルツ分光法による物性測定**
有機材料, 強誘電体、半導体、超伝導体
水、水溶液
- **非線型テラヘルツ分光の必要性と戦略**

Importance of terahertz frequency region



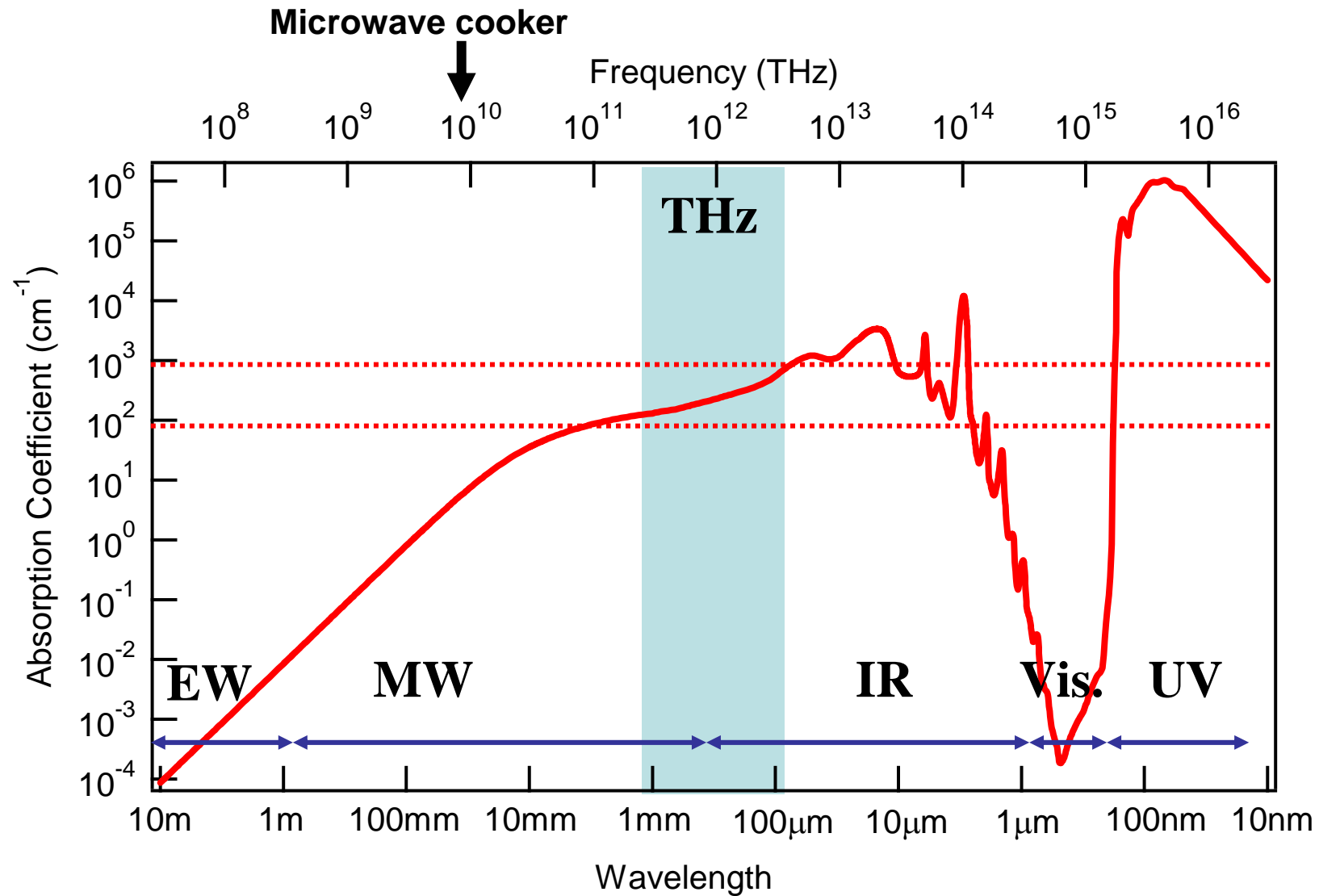
Radio wave

Infrared

Visible

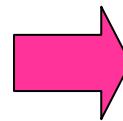
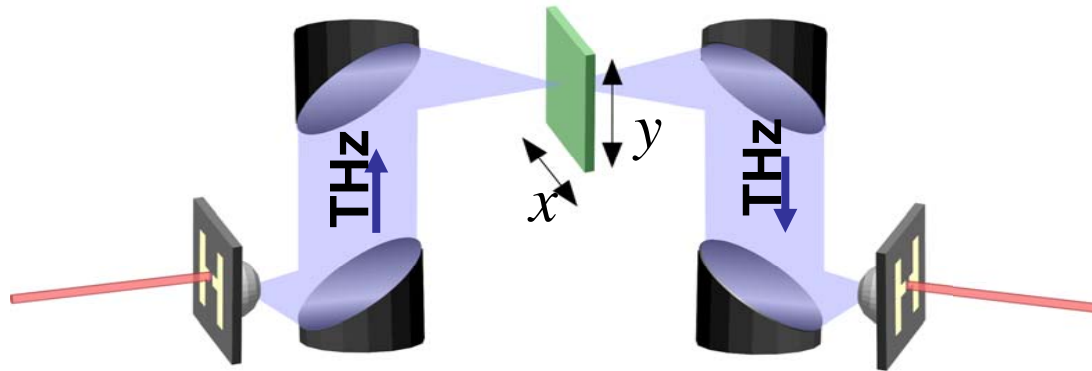


Absorption of Liquid Water



Jackson, Classical Electrodynamics

THz-Imaging

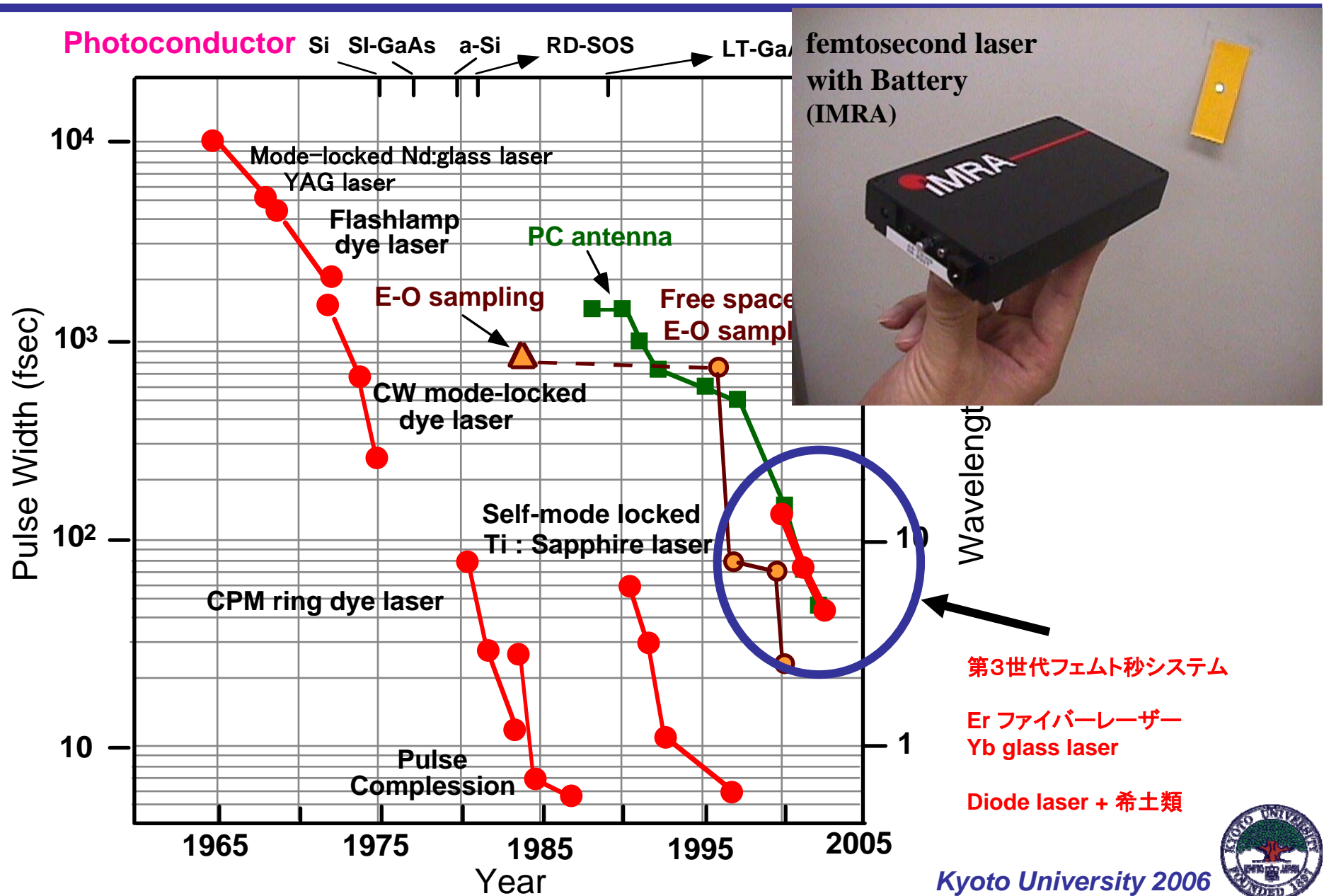


Much of current THz research revolves around spectral specificity and transmission properties. The THz frequency

講演内容

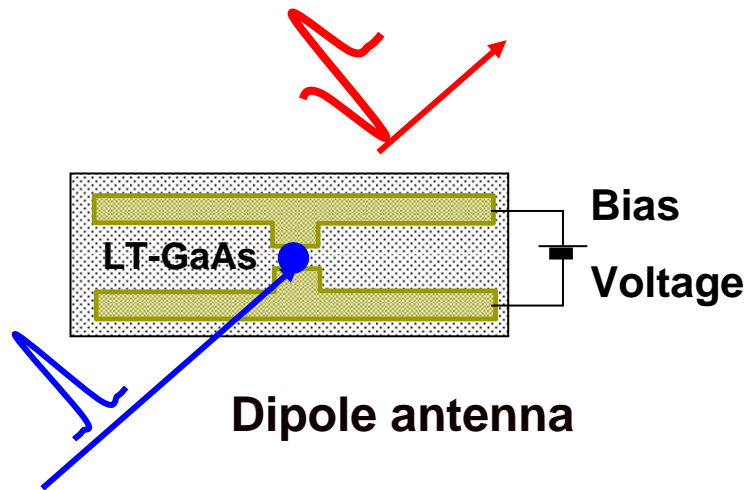
- テラヘルツテクノロジーとは何か？
- **時間領域テラヘルツ分光法の基礎**
- 時間領域テラヘルツ分光法による物性測定
有機材料, 強誘電体、半導体、超伝導体
水、水溶液
- 非線型テラヘルツ分光の必要性と戦略

THz-TDSの進展 - フェムト秒レーザーの進歩

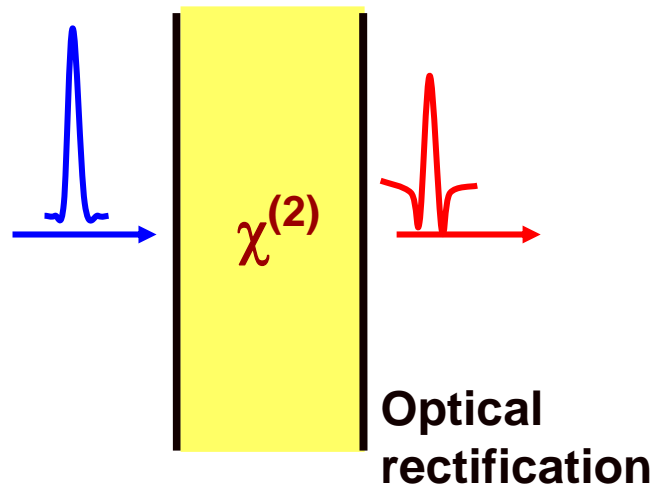


THz-detection

Generation



Dipole antenna



Optical rectification

Detection

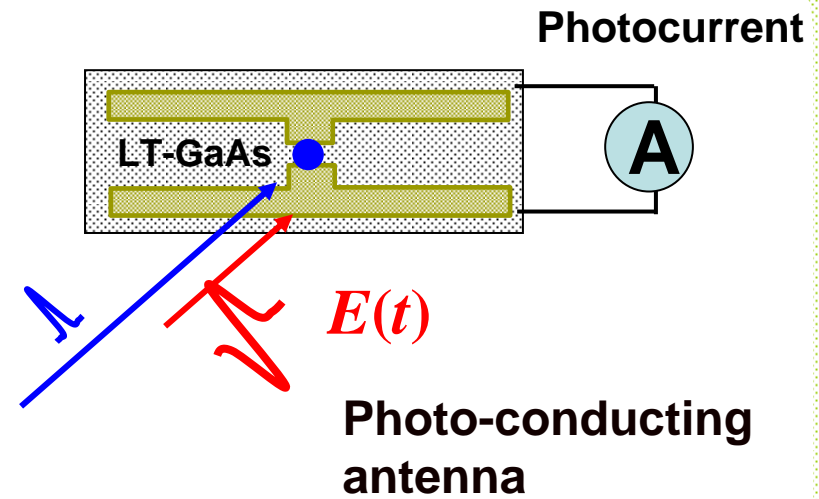
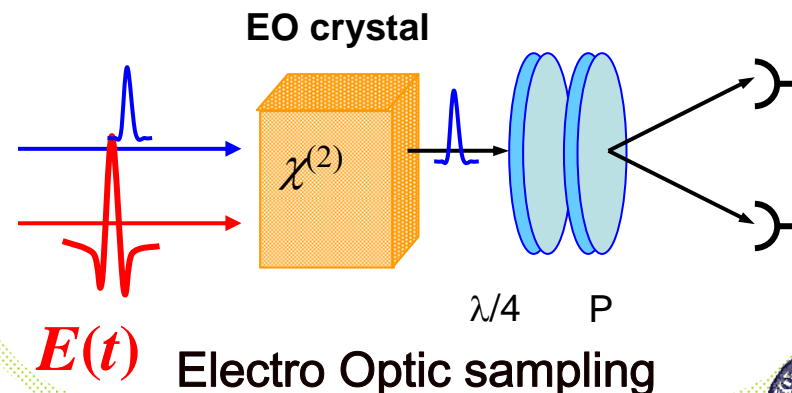
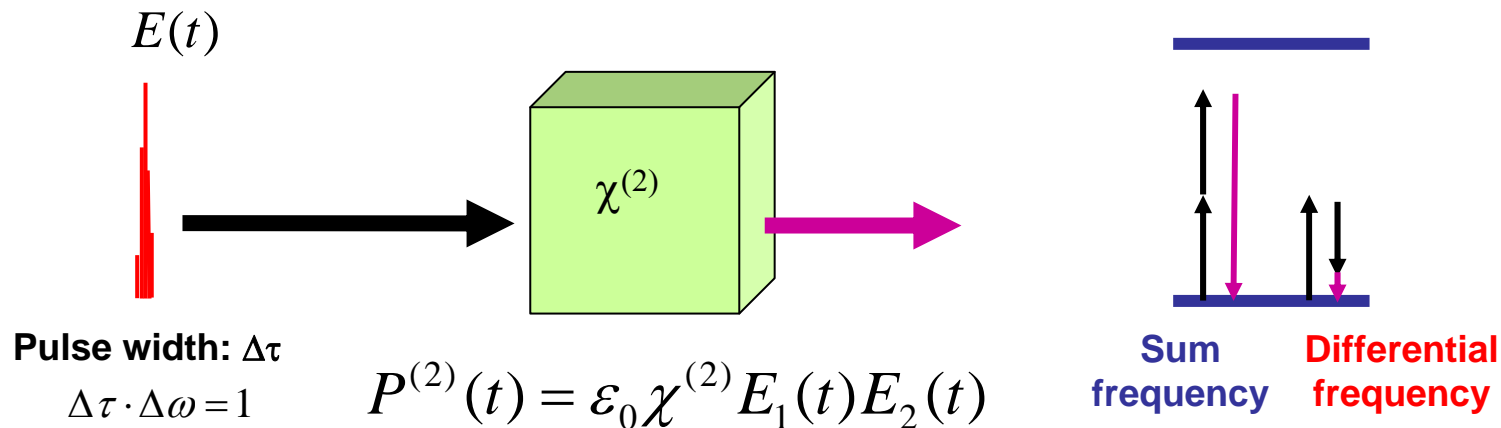


Photo-conducting antenna



Electro Optic sampling

THz-wave generation with second-order non-linear optical process



$$E_1(t) = E_2(t) = A(e^{i\omega t} + e^{-i\omega t})$$

$$P^{(2)}(t) = A^2 (\underbrace{\chi^{(2)}(2\omega, \omega, \omega)}_{\text{SHG}} e^{i2\omega t} + \underbrace{\chi^{(2)}(0, \omega, -\omega)}_{\text{Optical rectification}})$$

SHG

Optical rectification

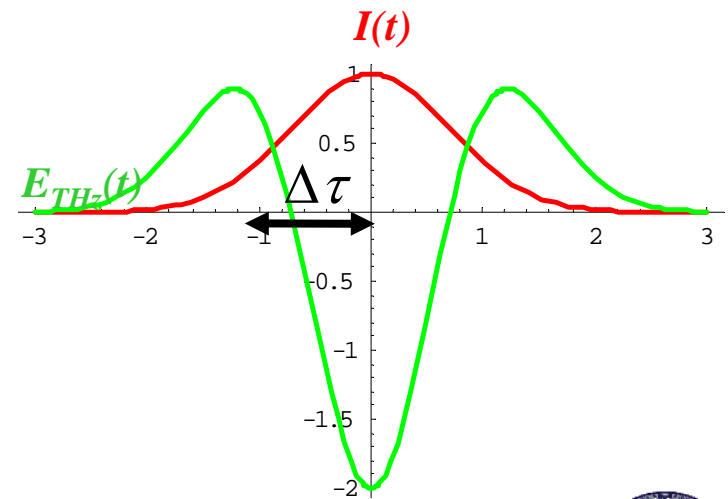
$$P^{(2)}(2\omega)$$

$$P^{(2)}(0)$$

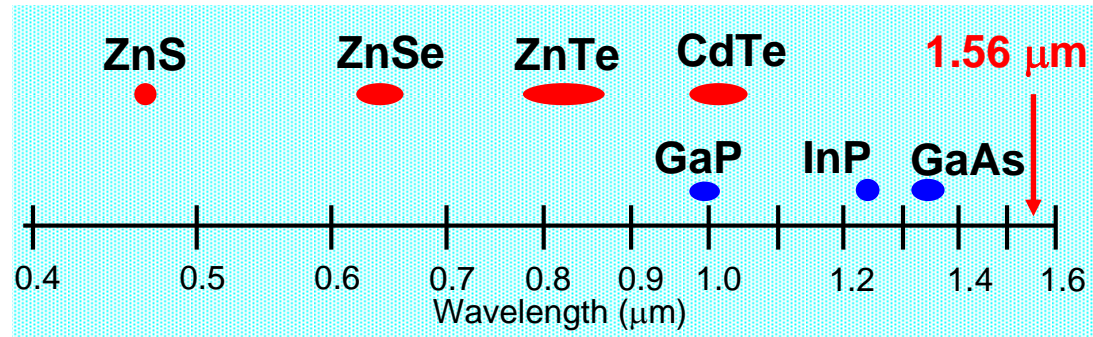
$$\Delta\tau \cdot \Delta\omega = 1$$

$$\Omega < \Delta\omega$$

$$P^{(2)}(t) = A^2 \chi^{(2)}(\Omega, \omega + \Omega, -\omega) e^{i\Omega t}$$



Phase matching condition



Phase match condition:

$$k(\omega+\Omega) - k(\omega) - k(\Omega) = 0$$

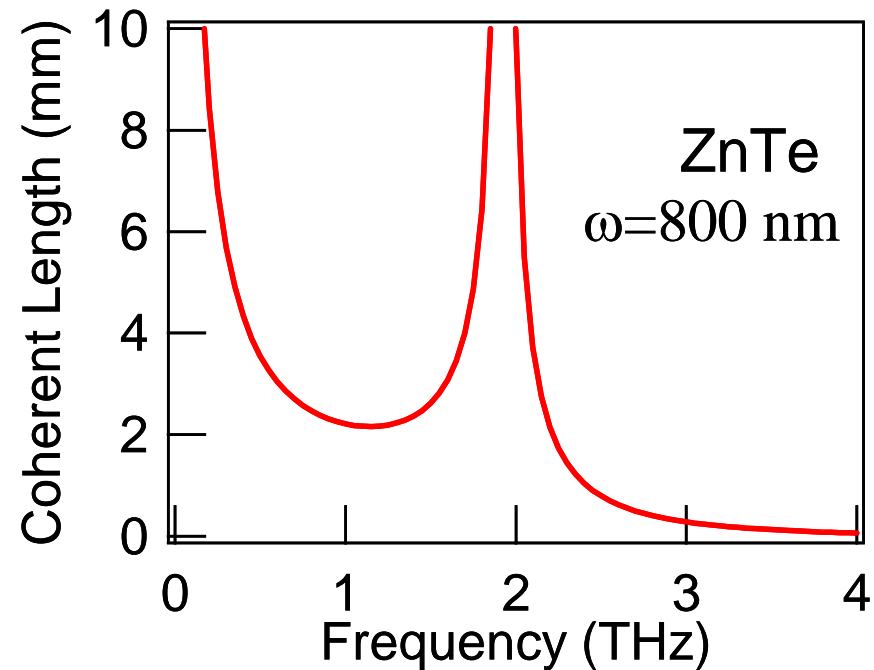
Including dispersion:

refractive index in THz region = optical Index of group velocity

$$V_{phase}^{THz} = V_{group}^{visible}$$

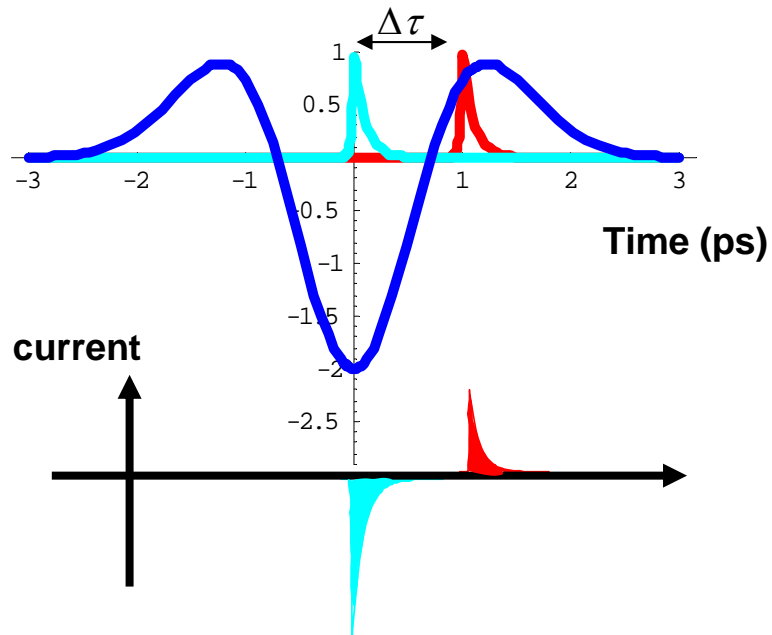
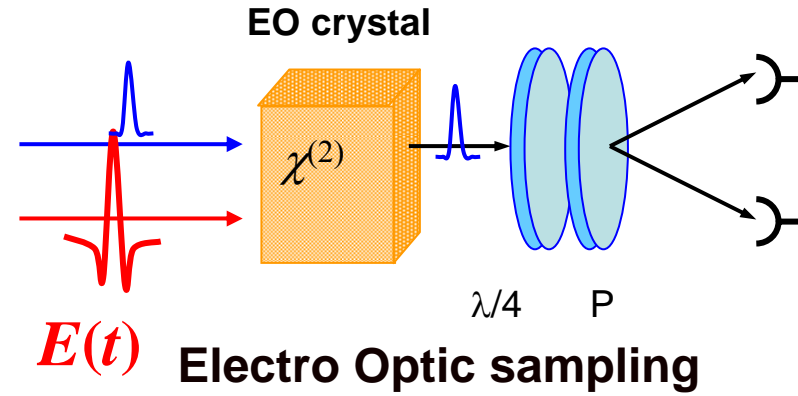
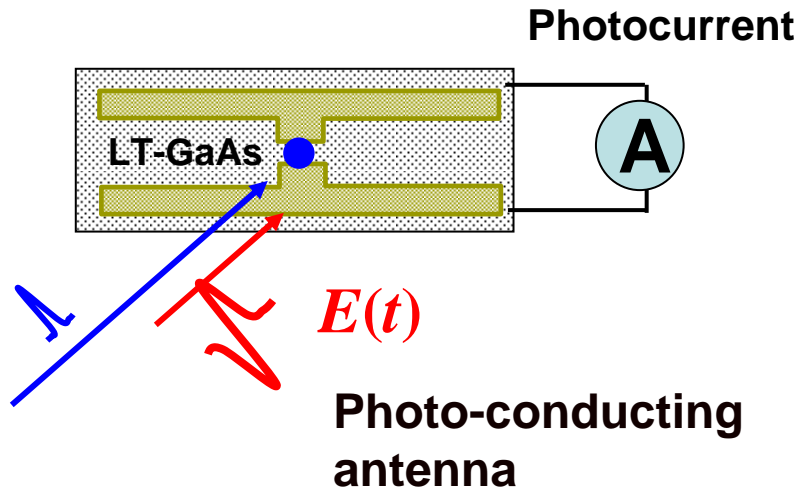
Coherent length:

$$l_c = \frac{c}{2f |n_{THz} - n_g|}$$



Nahata et al., APL **69**, 2321 (1996).

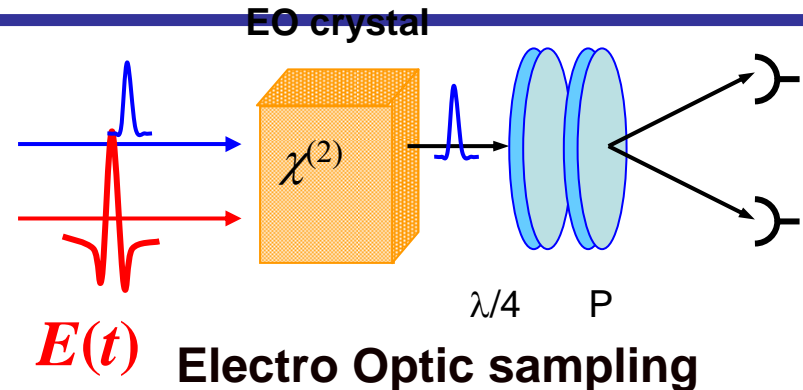
THz-wave detection



$$J(\Delta\tau) = e\mu \int_{-\infty}^{\infty} dt E^{THz}(t) N(t - \Delta\tau)$$

Non-linear THz spectroscopy

State of the art in our laboratory
(Kumiko YAMASHITA, 2005) :



– Estimation was made by EO sampling technique.

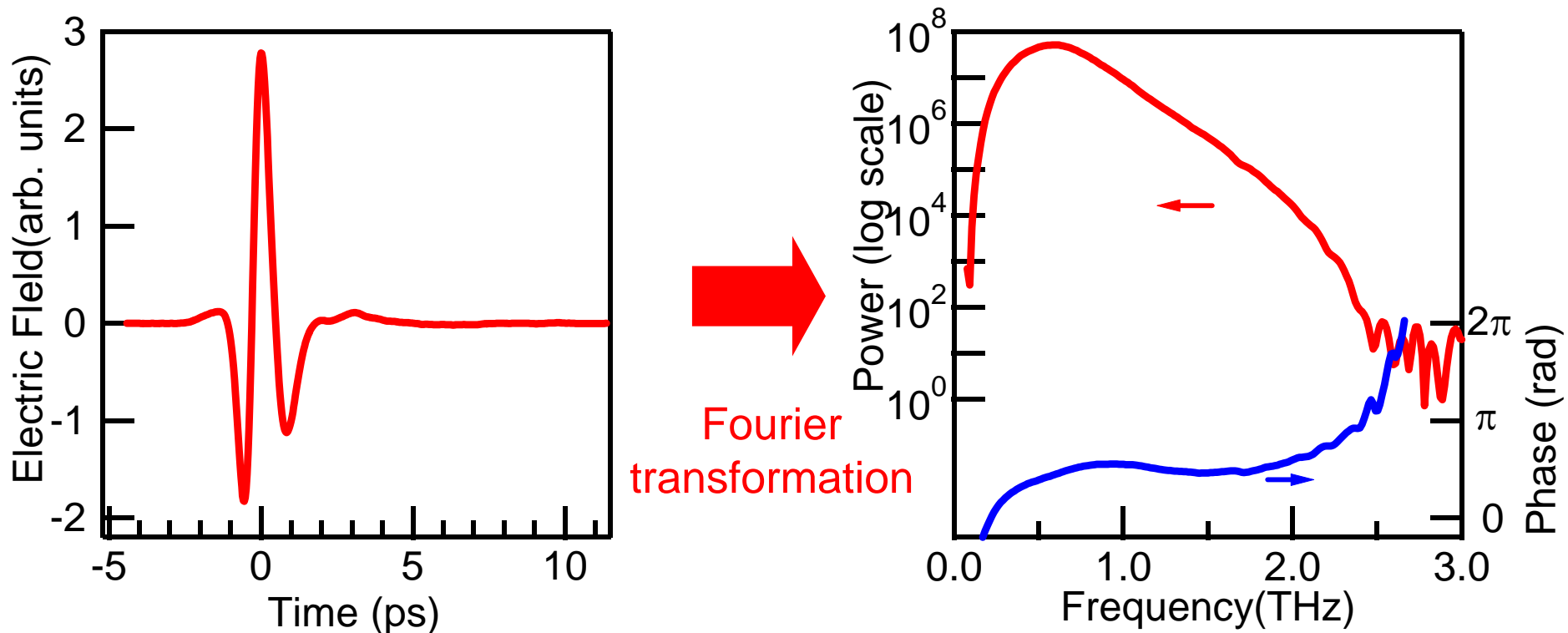
$$\frac{\Delta I}{I} = -\Gamma = -2\pi \frac{l}{\lambda} n^3 r_{41} |E_{THz}| = 0.2$$

Optical pump: $\lambda = 800\text{nm}$ 485 mW (485 μJ /pulse)
ZnTe($l=1\text{mm}$, $n=3.2$, $r_{41}=4 \times 10^{-12}\text{m/V}$)

$P_{THz} = 100 \text{ pJ/pulse}$, 10 nJ/cm^2 , 10 kW/cm^2 , $|E_{THz}| \sim 1\text{kV/cm} = 100\text{kV/m}$

*Typically, for the non-linear spectroscopy in visible region,
we need a MW/cm² class laser.*

Time-domain spectroscopy (TDS) is a powerful tool in THz region

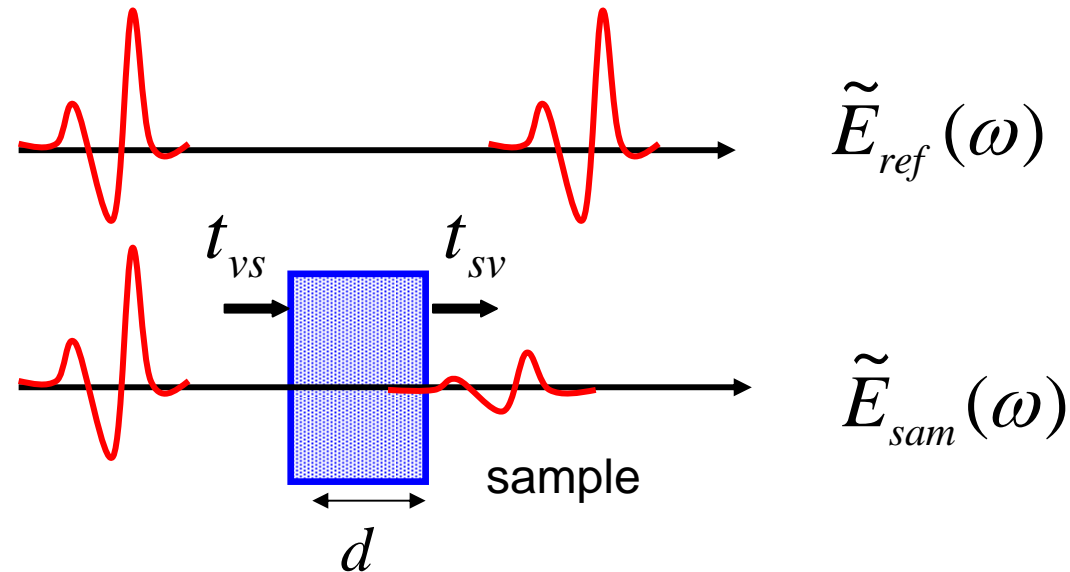


$$\tilde{E}(\omega) = E(\omega)e^{-i\phi(\omega)} = \frac{1}{2\pi} \int E(t)e^{i\omega t} dt$$

- ✓ Pulse measurements \Rightarrow High sensitivity. cf. FTIR
- ✓ Electric field measurements \Rightarrow Complex dielectric constants.

$$E(\omega), \quad \phi(\omega)$$

Terahertz Time-Domain Spectroscopy (THz-TDS)



$$\begin{aligned}\tilde{t}(\omega) &= \frac{\tilde{E}_{sam}(\omega)}{\tilde{E}_{ref}(\omega)} \\ &= t_{vs} \cdot t_{sv} \exp\left[i \frac{(\tilde{n}(\omega) - 1)\omega d}{c}\right] \\ &= t_{vs} \cdot t_{sv} \exp\left[i \frac{(n-1)\omega d}{c}\right] \exp\left[-\frac{\kappa\omega d}{c}\right]\end{aligned}$$

Complex refractive index

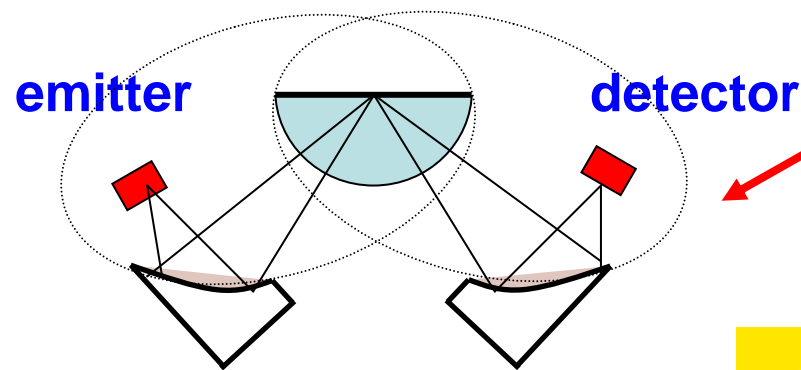
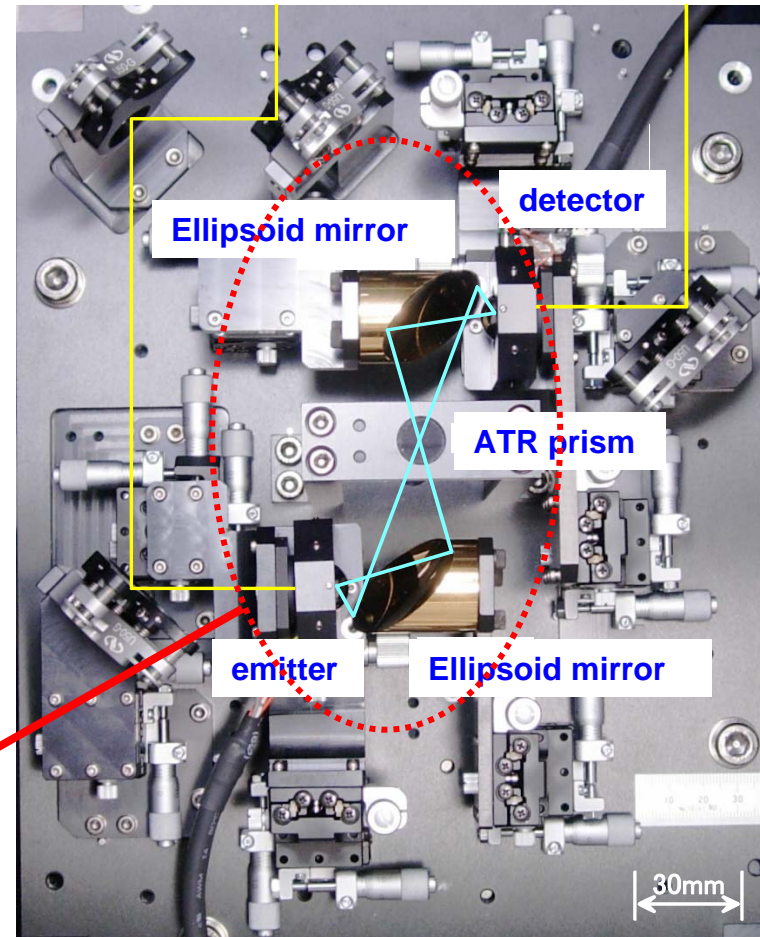
$$\tilde{n} = n + i\kappa$$

t_{vs}, t_{sv} : Fresnel coefficients

$$t_{vs} = \frac{2}{\tilde{n}(\omega) + 1} \quad (\text{vacuum} \rightarrow \text{sample})$$

$$t_{sv} = \frac{2\tilde{n}(\omega)}{\tilde{n}(\omega) + 1} \quad (\text{sample} \rightarrow \text{vacuum})$$

Compact THz-ATR spectrometer



Double-ellipsoid mirrors with a semispherical ATR prism.



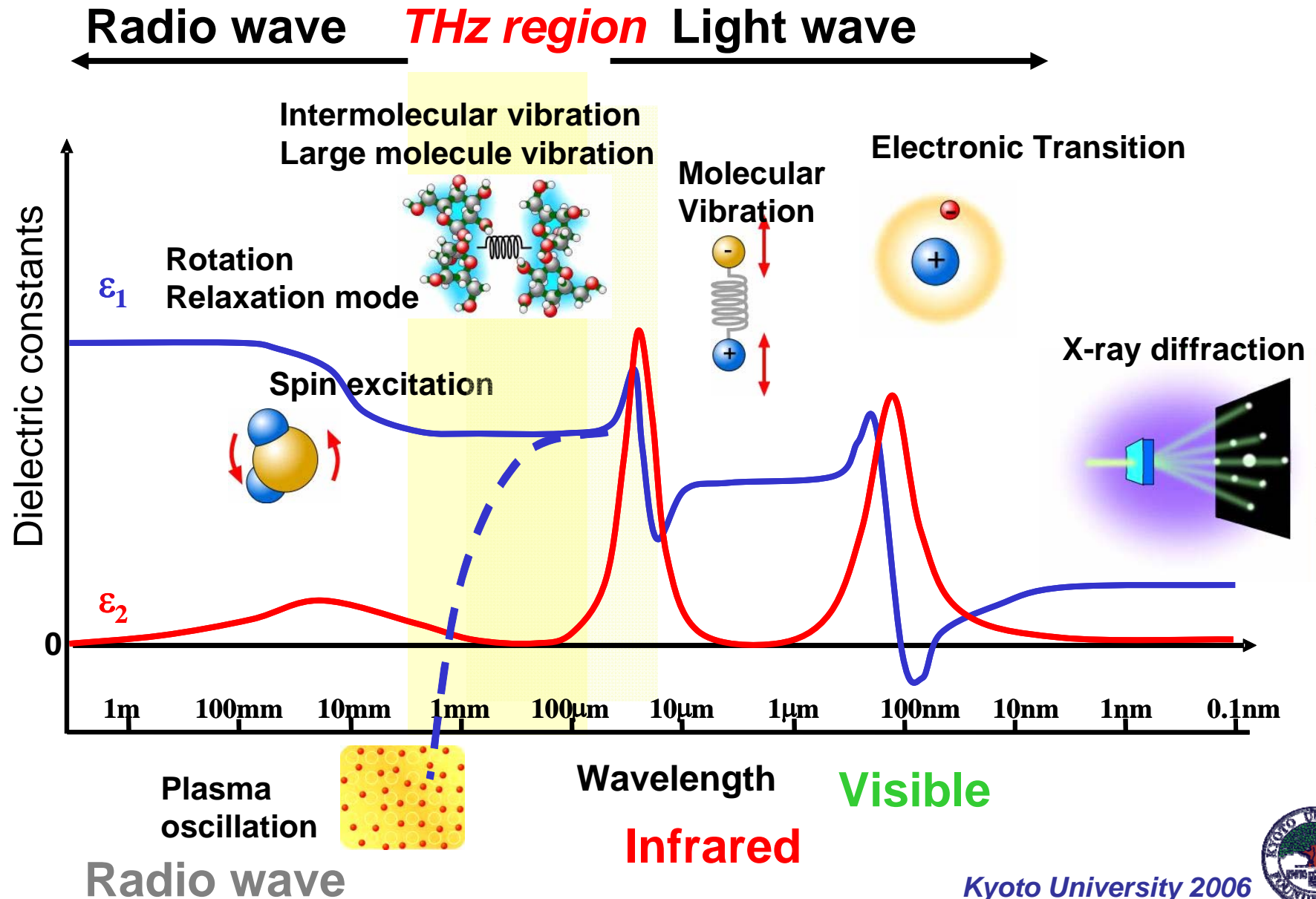
Advanced Terahertz Technologies adapted for Optical Communication



講演内容

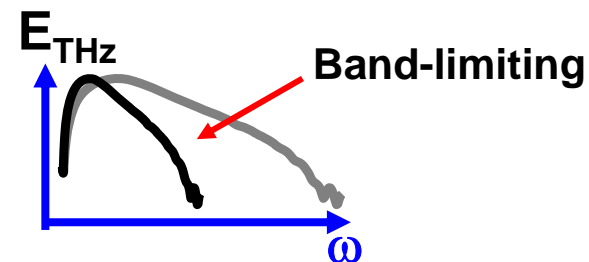
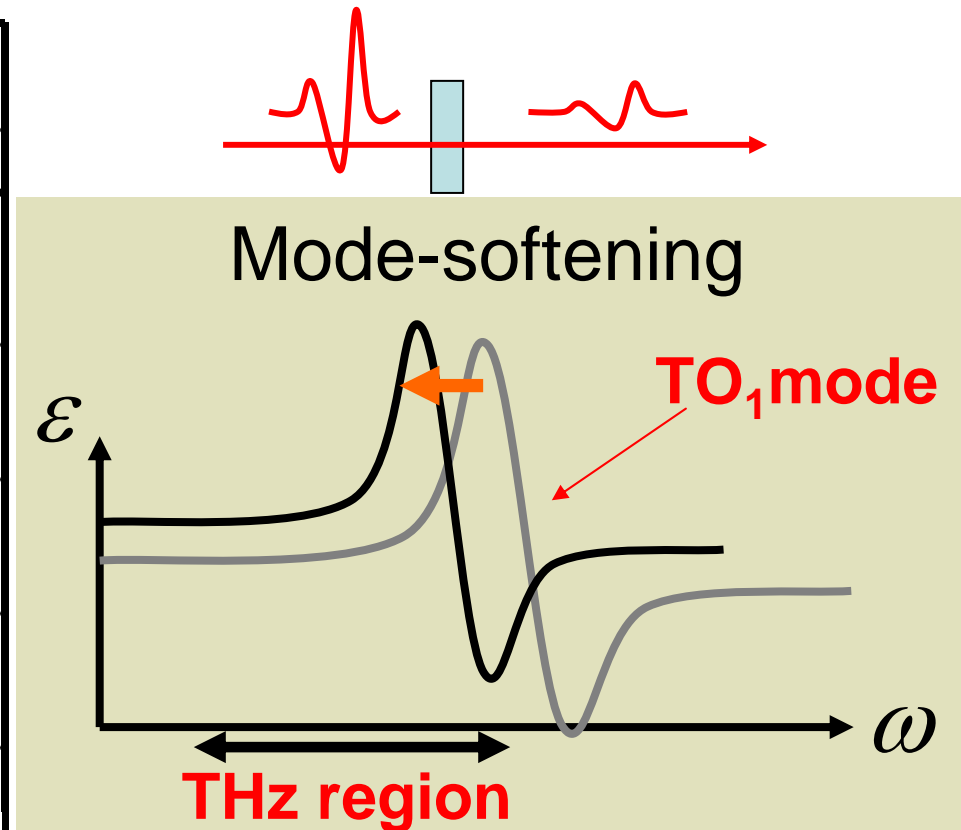
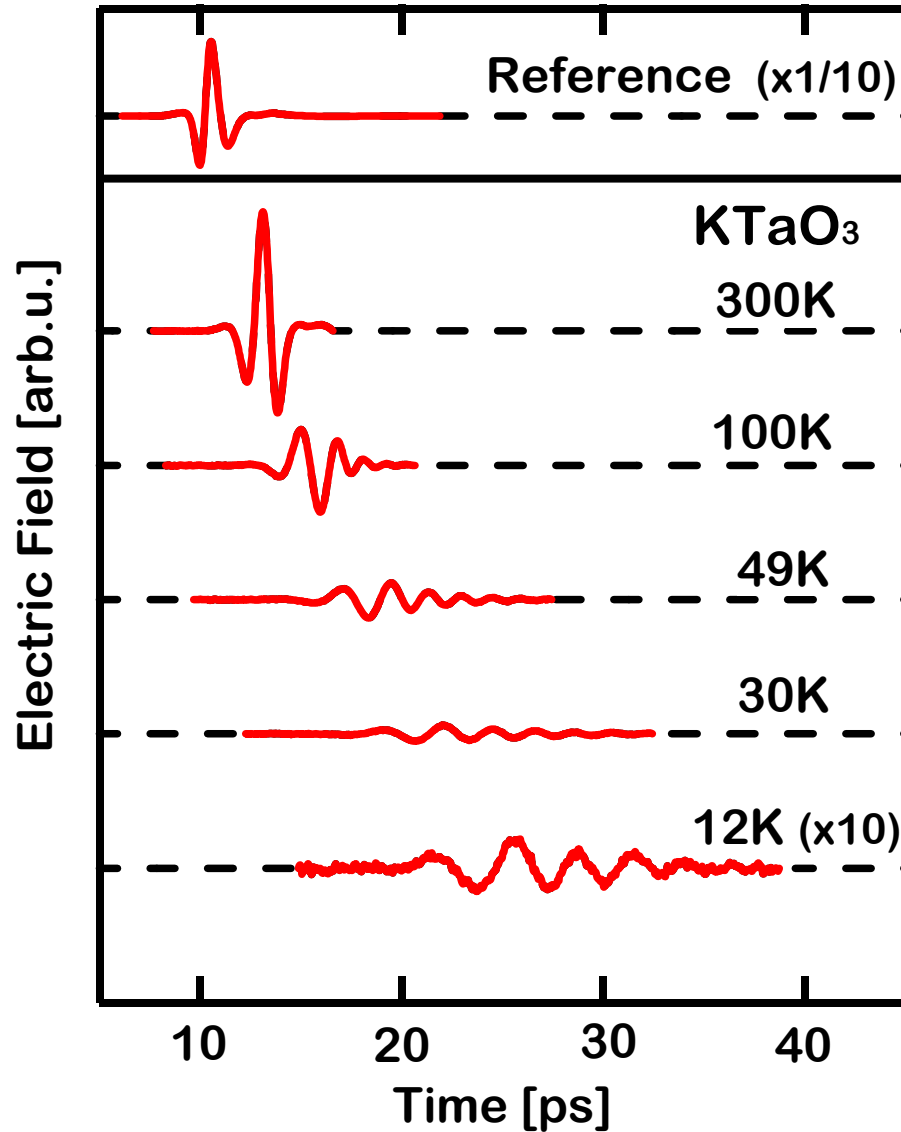
- テラヘルツテクノロジーとは何か？
- 時間領域テラヘルツ分光法の基礎
- **時間領域テラヘルツ分光法による物性測定**
有機材料, 強誘電体、半導体、超伝導体
水、水溶液
- 非線型テラヘルツ分光の必要性と戦略

Importance of terahertz frequency region



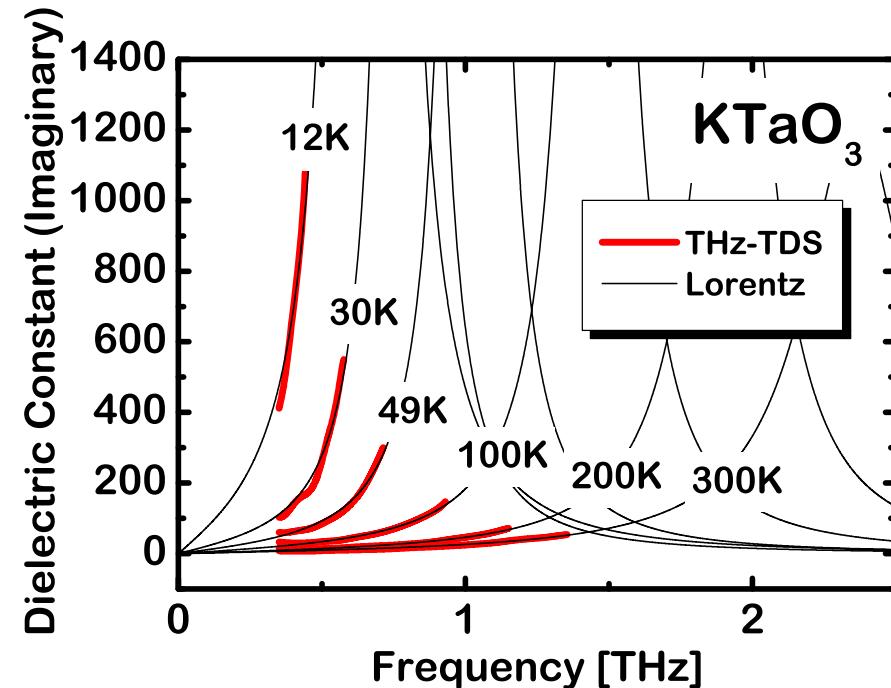
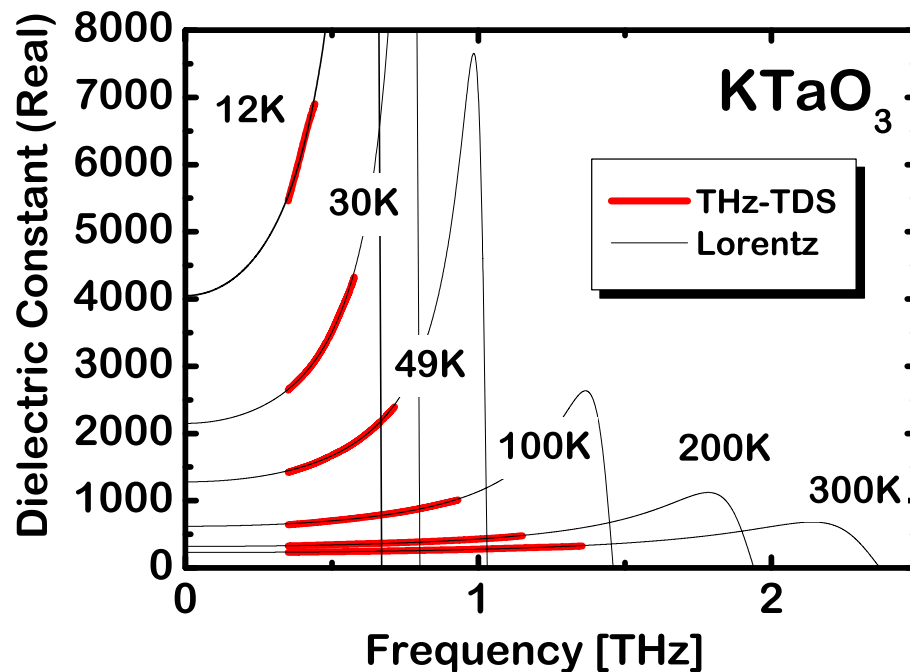
Mode-softening in $KTaO_3$ crystal

Ichikawa, Tanaka *et al.*: Physical Review B 71(2005) 086509.



Dielectric function in KTaO_3

Ichikawa et al.: Physical Review B 71(2005) 086509.



A single Lorentz Model

$$\tilde{\epsilon}(\omega) = \epsilon_{\infty} + \frac{(\epsilon_0 - \epsilon_{\infty})\Omega_0^2}{\Omega_0^2 - \omega^2 - i\gamma_0\omega}$$

Fitting parameters

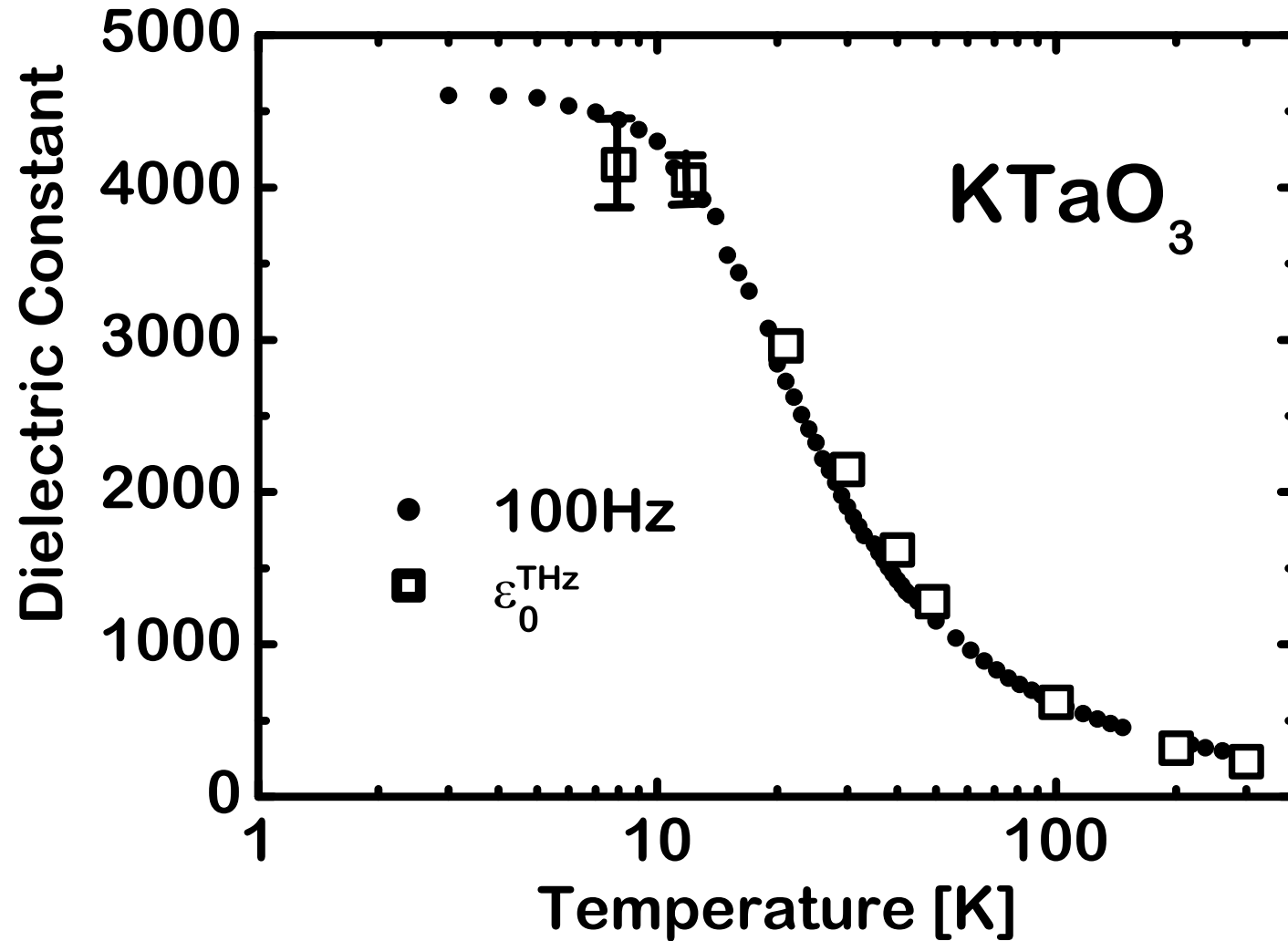
Ω_0 : Mode frequency

γ_0 : Damping

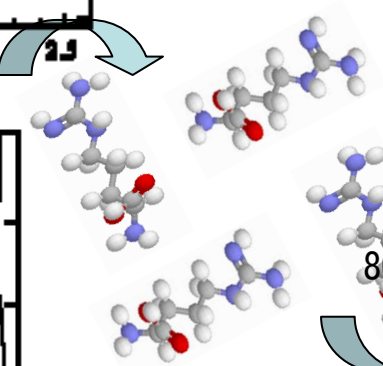
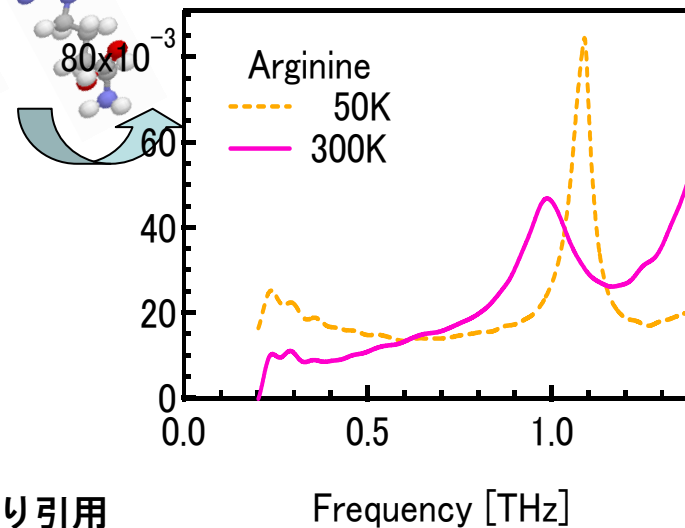
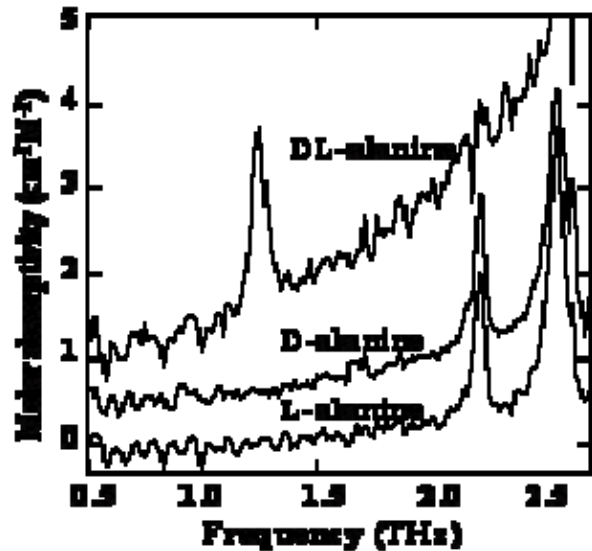
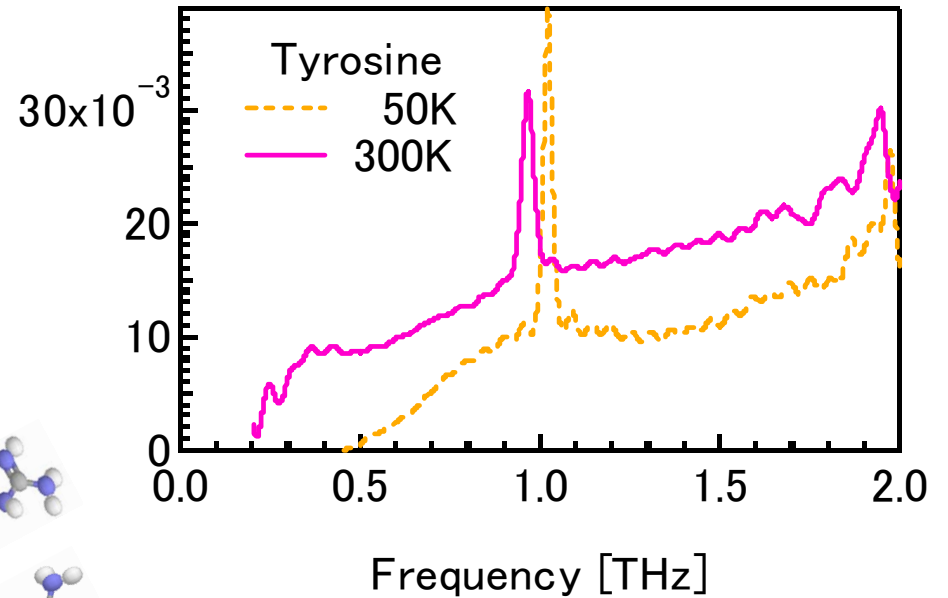
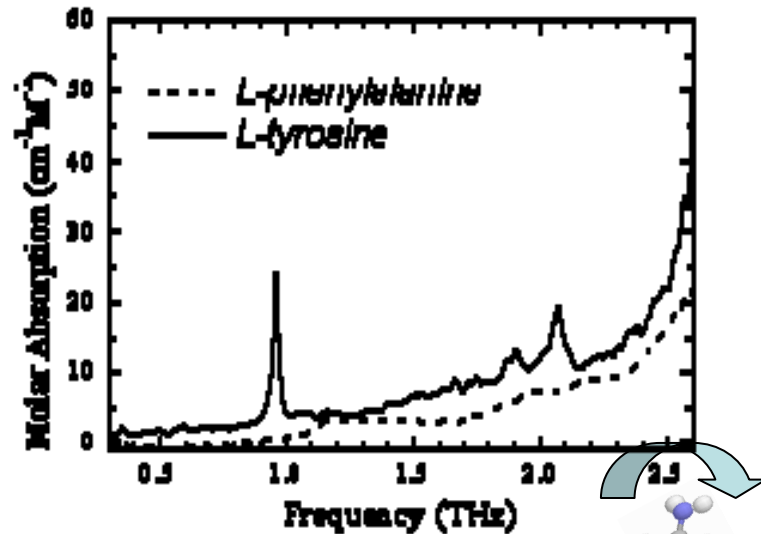
ϵ_0 : Static dielectric constant

Static dielectric constant

Ichikawa et al.: Physical Review B 71(2005) 086509.



アミノ酸結晶の吸収



谷他、「アミノ酸分子結晶のテラヘルツ時間領域分光」より引用

http://www.technova.co.jp/teratech/saizensen/tera_saizensen1.html

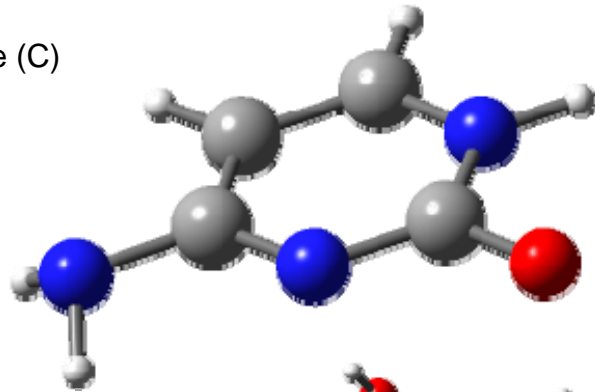
Frequency [THz]

Kyoto University 2006

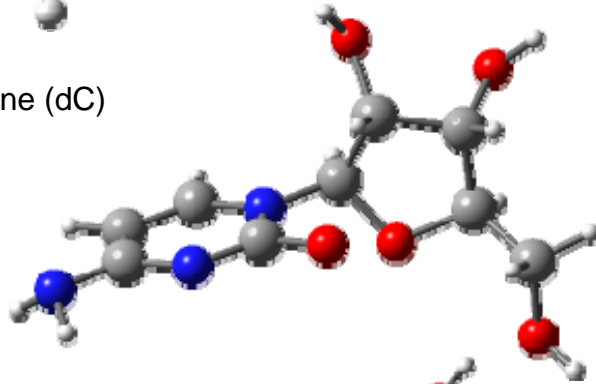


isolated bases → DNA: first step

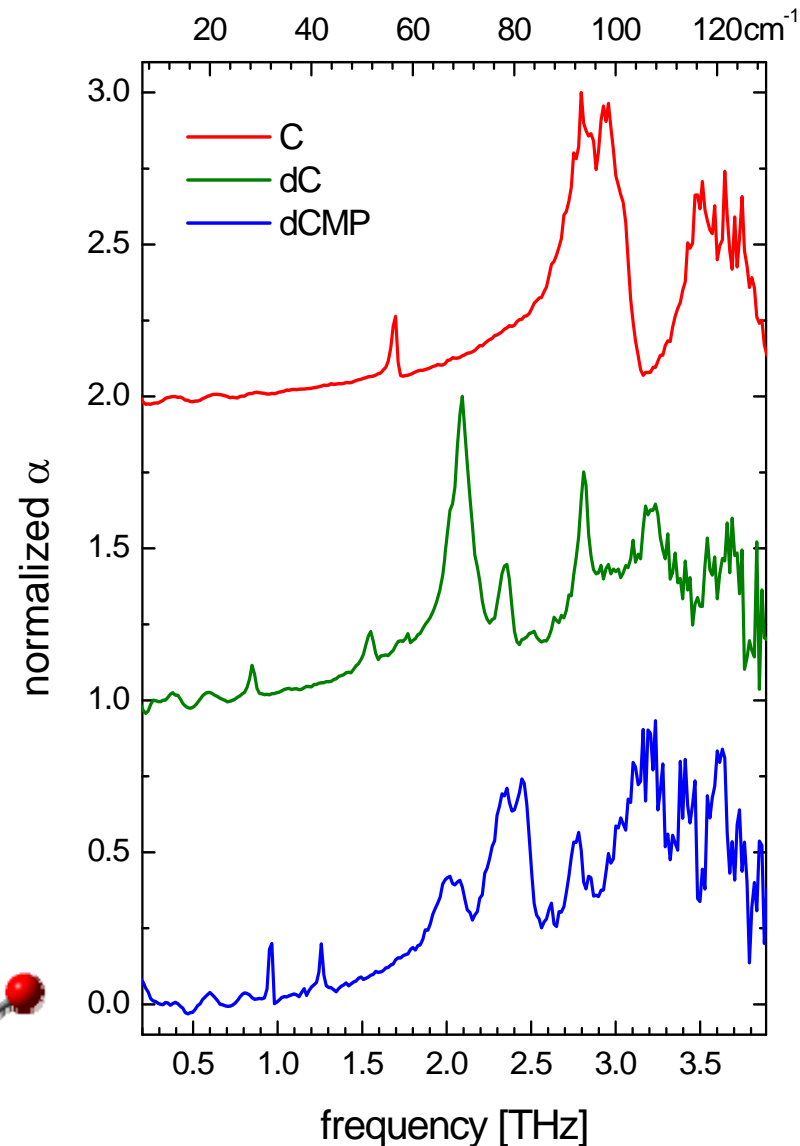
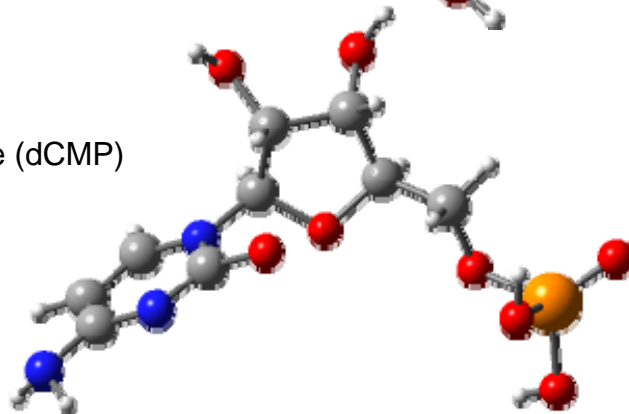
cytosine (C)



deoxycytidine (dC)



deoxycytidine-
monophosphate (dCMP)

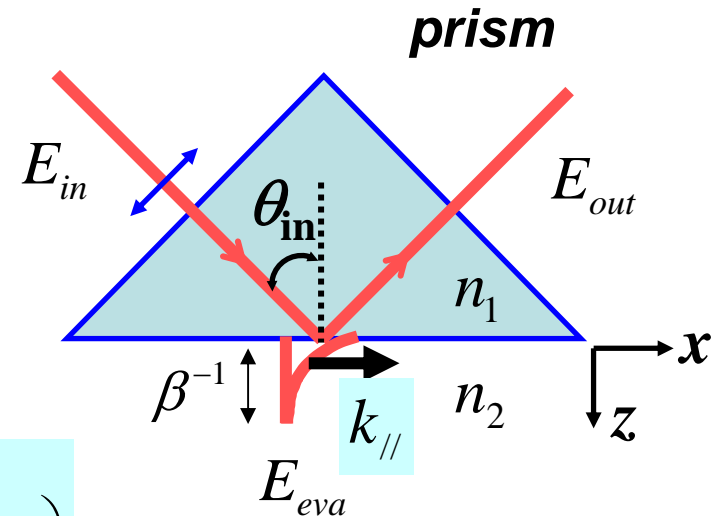


Evanescent wave in ATR

Internal total reflection condition

Evanescent wave
for p -polarization

$$\theta_{in} > \theta_c = \text{Sin}^{-1}\left(\frac{n_2}{n_1}\right)$$



$$\begin{pmatrix} H_x \\ H_y \\ H_z \end{pmatrix} = \begin{pmatrix} 0 \\ \underline{B} \\ 0 \end{pmatrix} \exp(-\beta z) \exp i \left(\frac{n_1 k \sin \theta_{in}}{n_2} x - \omega t \right)$$

TM mode

$$E_{eva} \begin{pmatrix} E_x \\ E_y \\ E_z \end{pmatrix} = \begin{pmatrix} A \\ 0 \\ C \end{pmatrix} \exp(-\beta z) \exp i \left(\frac{n_1 k \sin \theta_{in}}{n_2} x - \omega t \right)$$

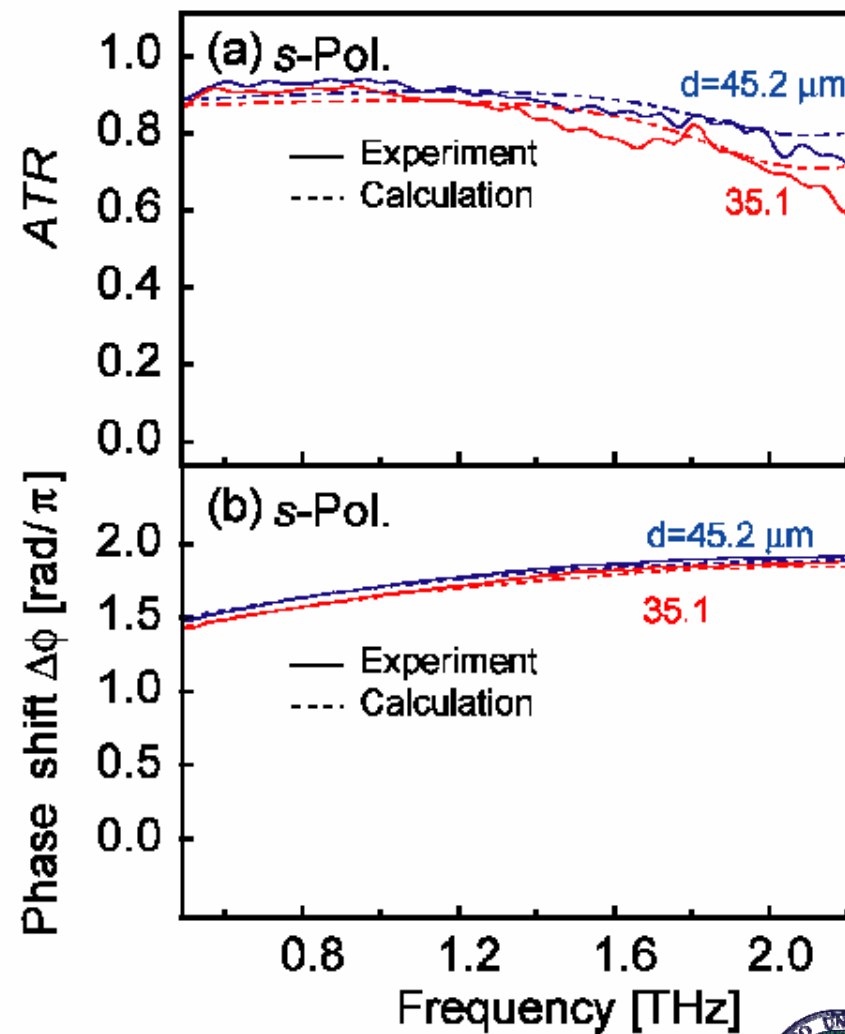
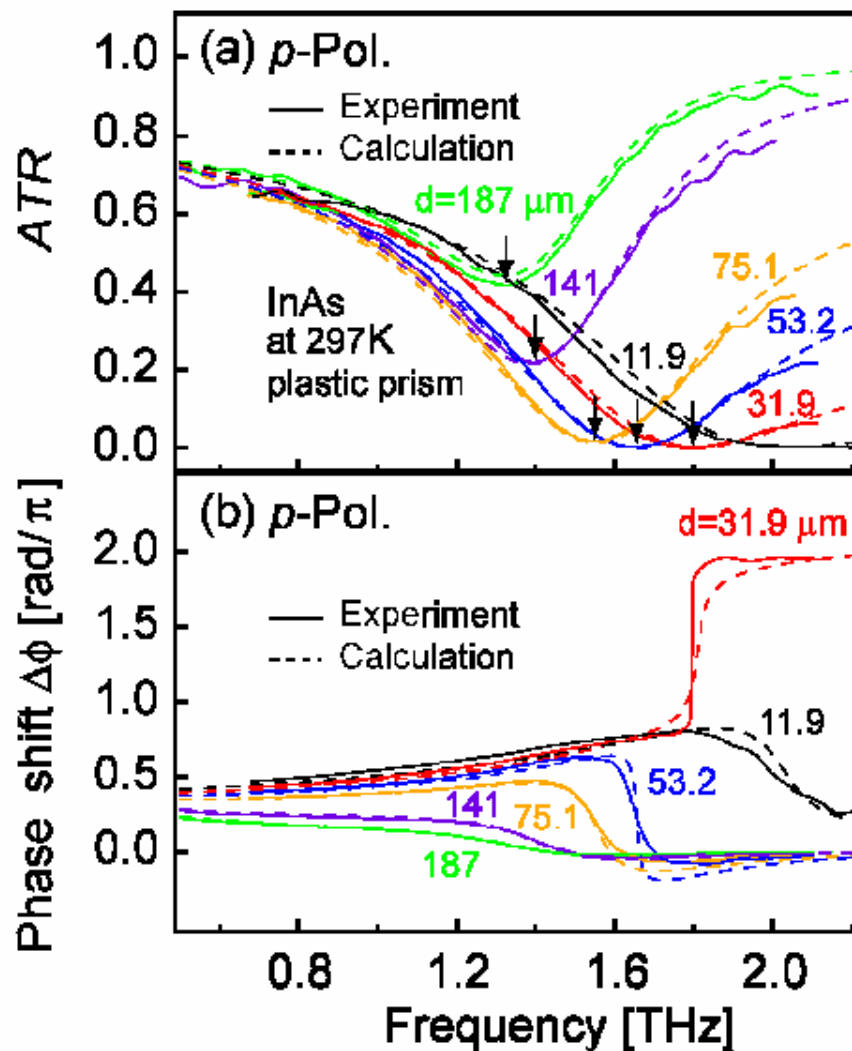
TM mode with large $k_{//}$

Enable to excite
surface modes.

exponentially decaying
away from the interface waves

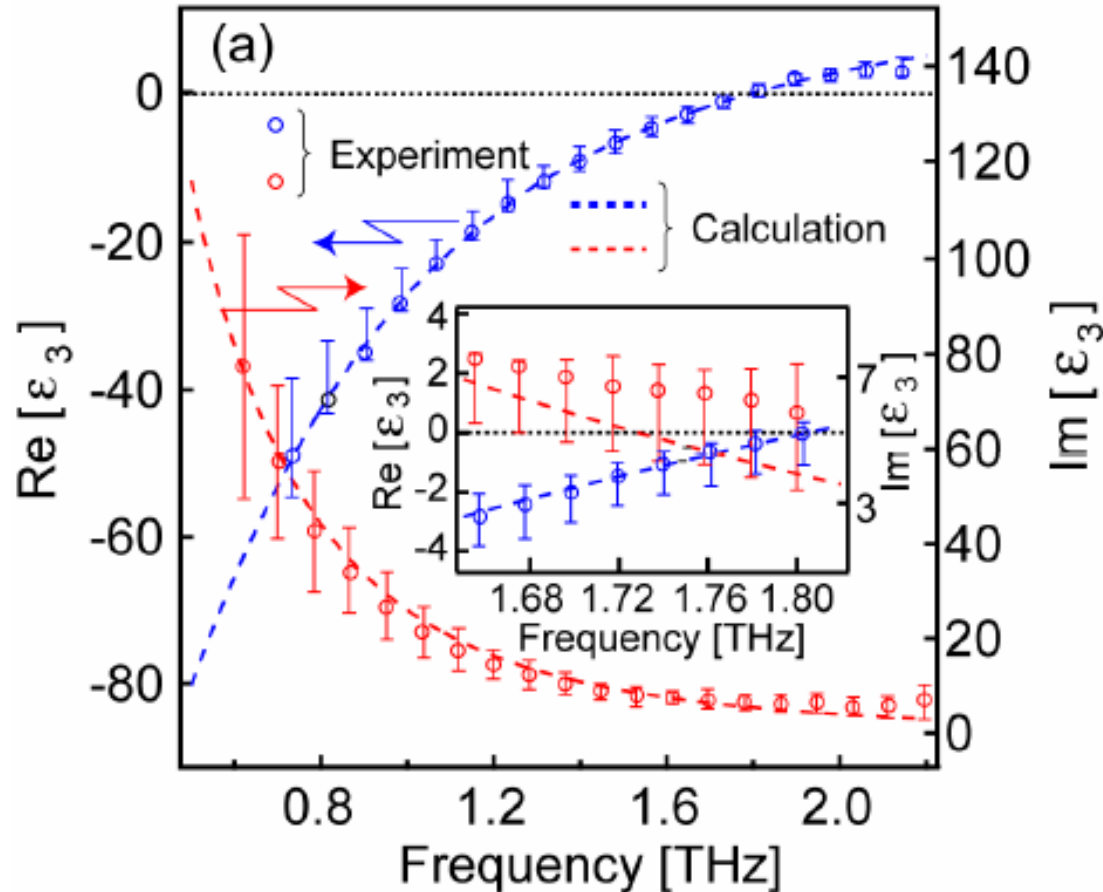
Surface plasmon in semiconductor with THz-ATR

H. Hirori, M. Nagai, and K. Tanaka, Optics Express, 13, (26), 10801-10814 (2005).

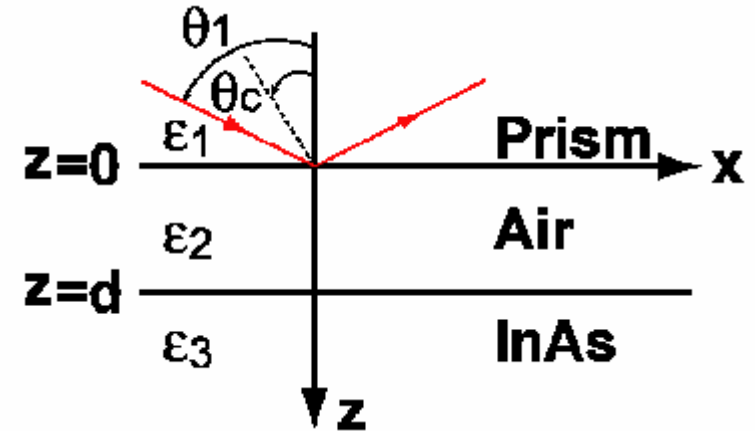


Dielectric constant in doped semiconductor

InAs n-type $n \sim 10^{17}$



Attenuated Total Reflection



$$\epsilon(\omega) = \epsilon_b \left(1 - \frac{\omega_p^2}{\omega(\omega + i\gamma)} \right)$$

$$\omega \ll \gamma$$

$$\epsilon(\omega) = i \frac{\epsilon_b \omega_p^2}{\gamma} \frac{1}{\omega} = i \frac{\sigma}{\omega}$$

H. Hirori, M. Nagai, and K. Tanaka, Optics Express, 13, (26), 10801-10814 (2005).

Kyoto University 2006

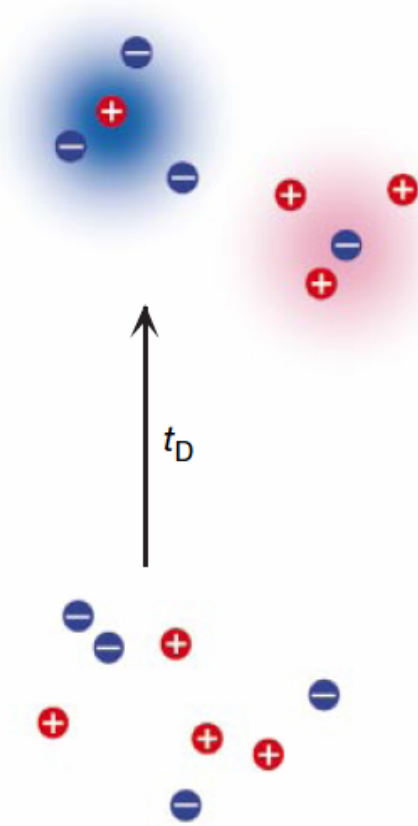
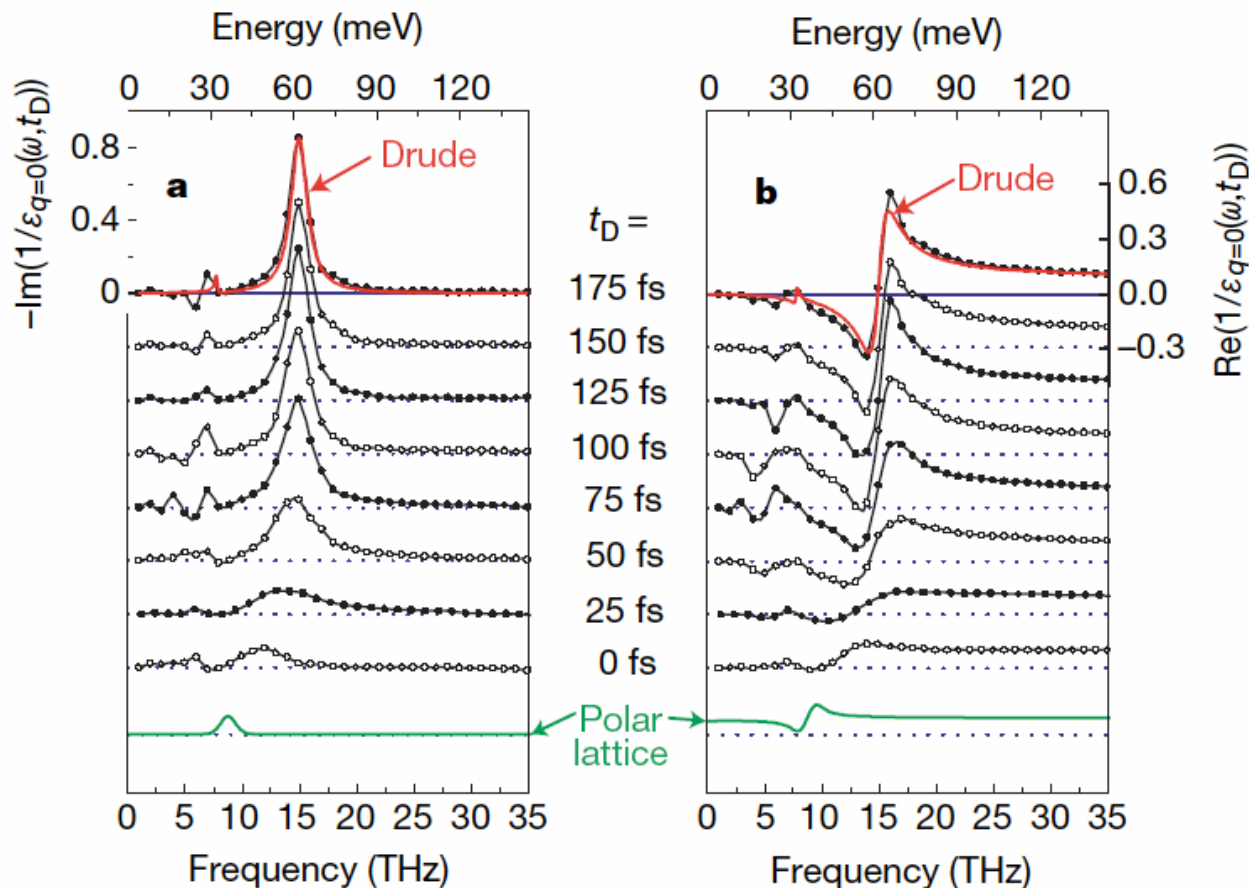


Pump and probe spectroscopy

“How many-particle interactions develop after ultrafast excitation of electron-hole plasma ”

R. Huber, F. Tauser, A. Brodschelm, M. Bichler, G. Abstreiter and A. Leitenstorfer

Nature. Vol.414 (2001) 286

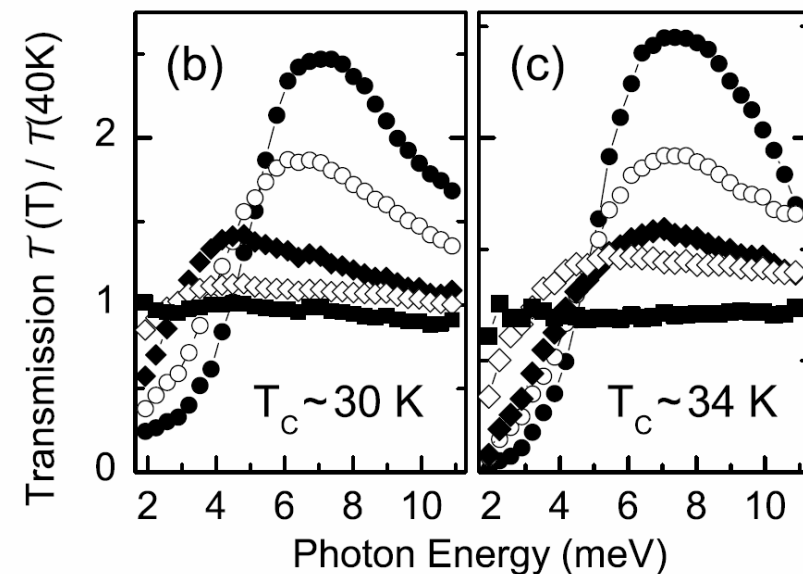
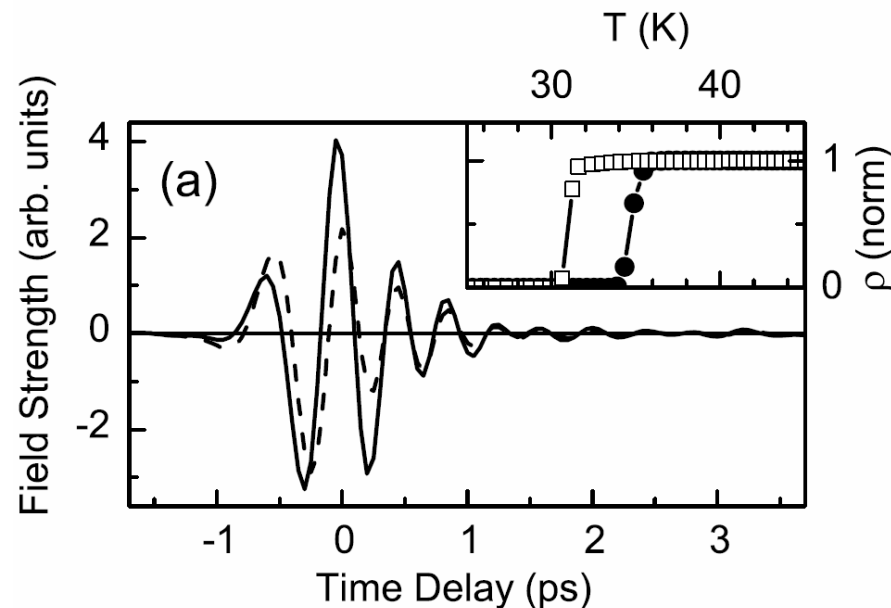


Superconducting gap

“Far-infrared optical conductivity gap in superconducting MgB₂ films”

R. A. Kaindl, M. A. Carnahan, J. Orestein, D. S. Chemla, H. M. Christen, H. Y. Zhai, M. Paranthaman and D. H. Lowndes

[Phys. Rev. Lett. 88 \(2002\) 027003](#)



100nm MgB₂薄膜における透過波形
6K(実線)と40K(破線)
Insetは100nm MgB₂薄膜(□)と200nm
MgB₂薄膜(●)の抵抗の温度変化

40Kの値で規格化した透過率

(b)膜厚100nm MgB₂

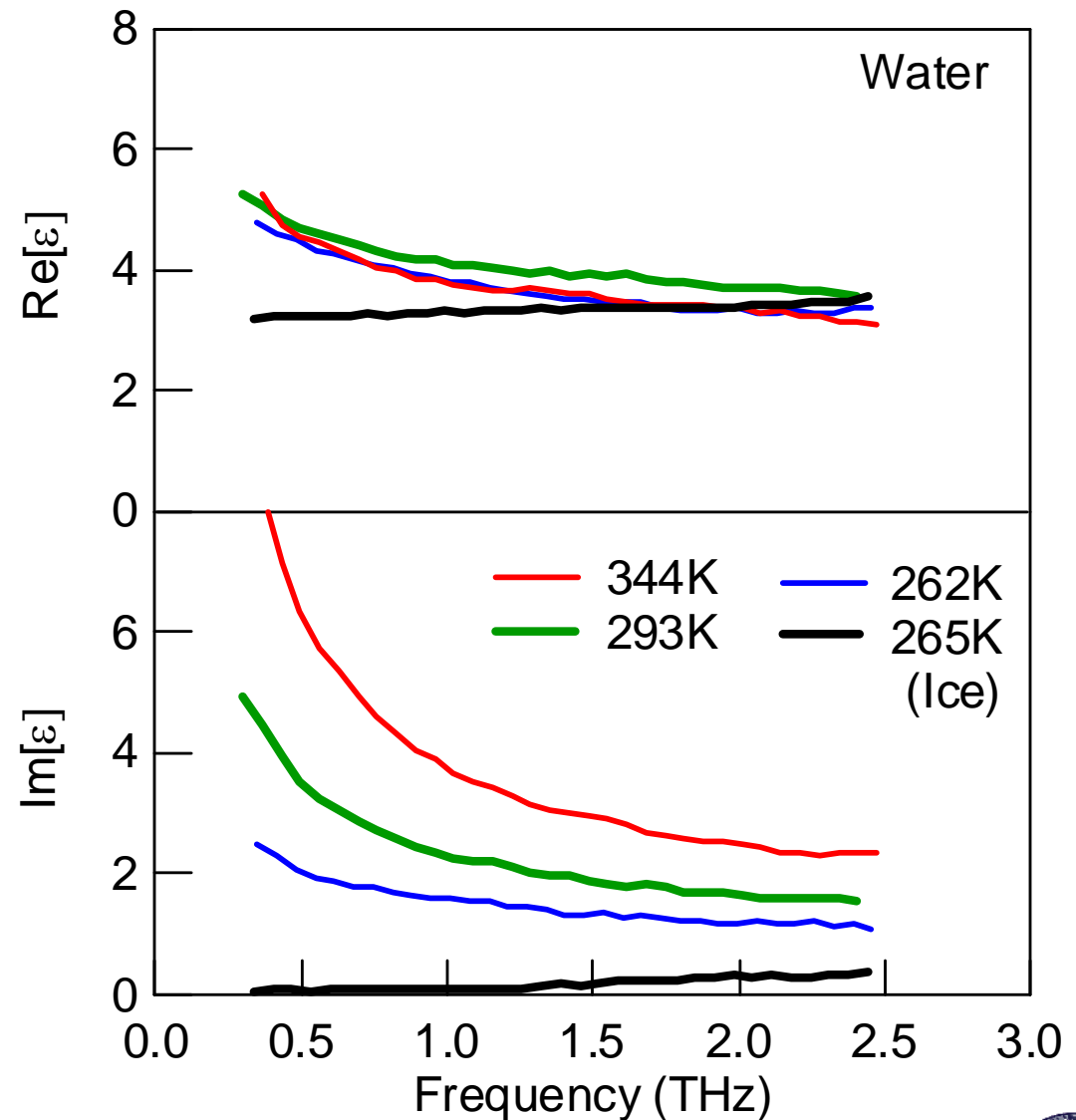
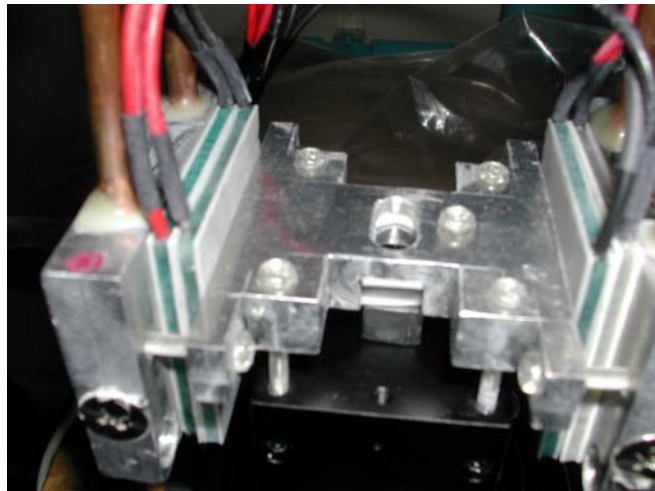
6K(●), 20K(○) 27K(◆), 30K(◇), 33K(■)

(c)膜厚200nm MgB₂(6K, 20K 25K, 30K, 36K)

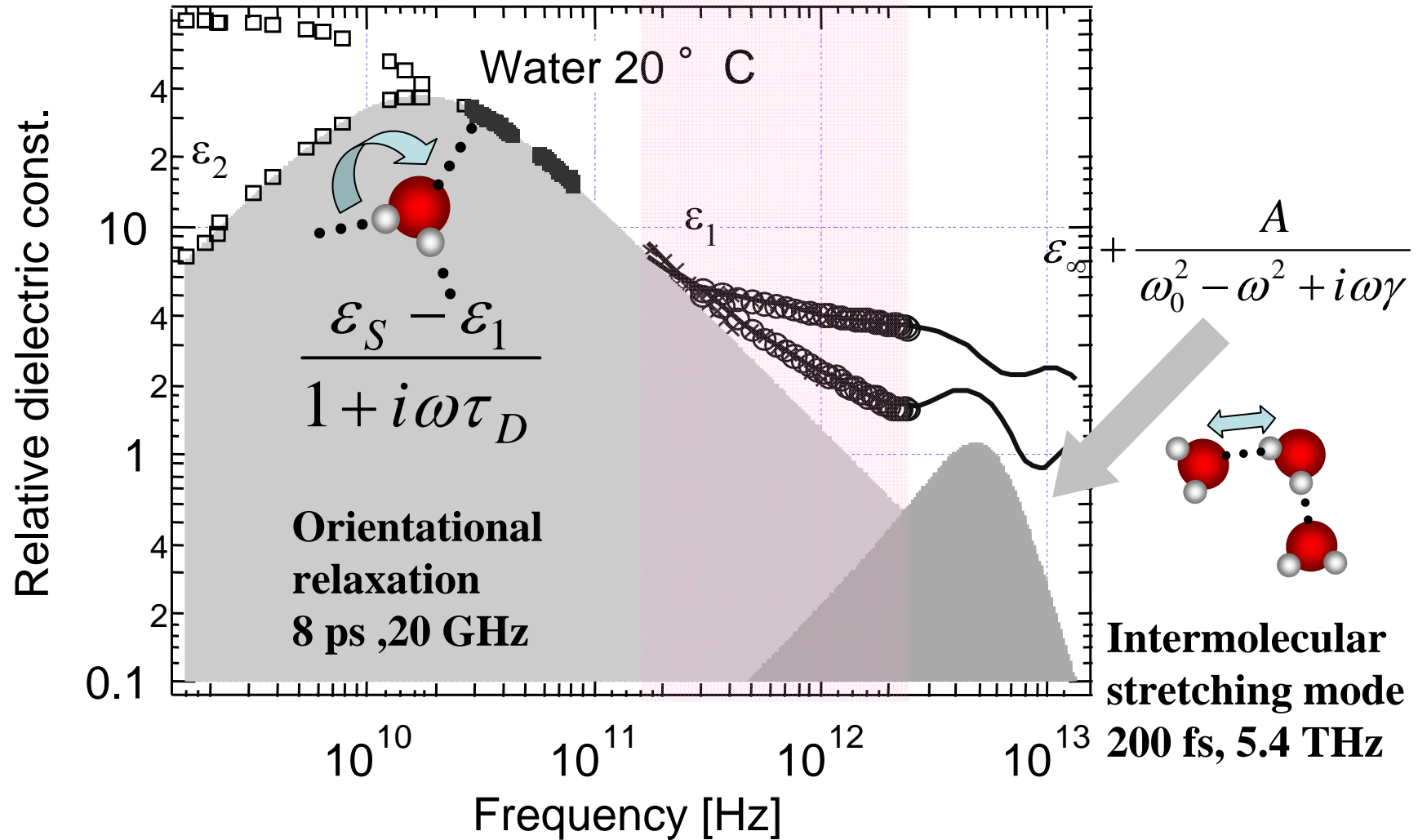
6K(●), 20K(○) 25K(◆), 30K(◇), 36K(■)

TD-ATR spectroscopy in water

Temperature-controlled
Si ATR prism



Dielectric Constants in Water



講演内容

- テラヘルツテクノロジーとは何か？
- 時間領域テラヘルツ分光法の基礎
- 時間領域テラヘルツ分光法による物性測定
有機材料, 強誘電体、半導体、超伝導体
水、水溶液
- 非線型テラヘルツ分光の必要性と戦略

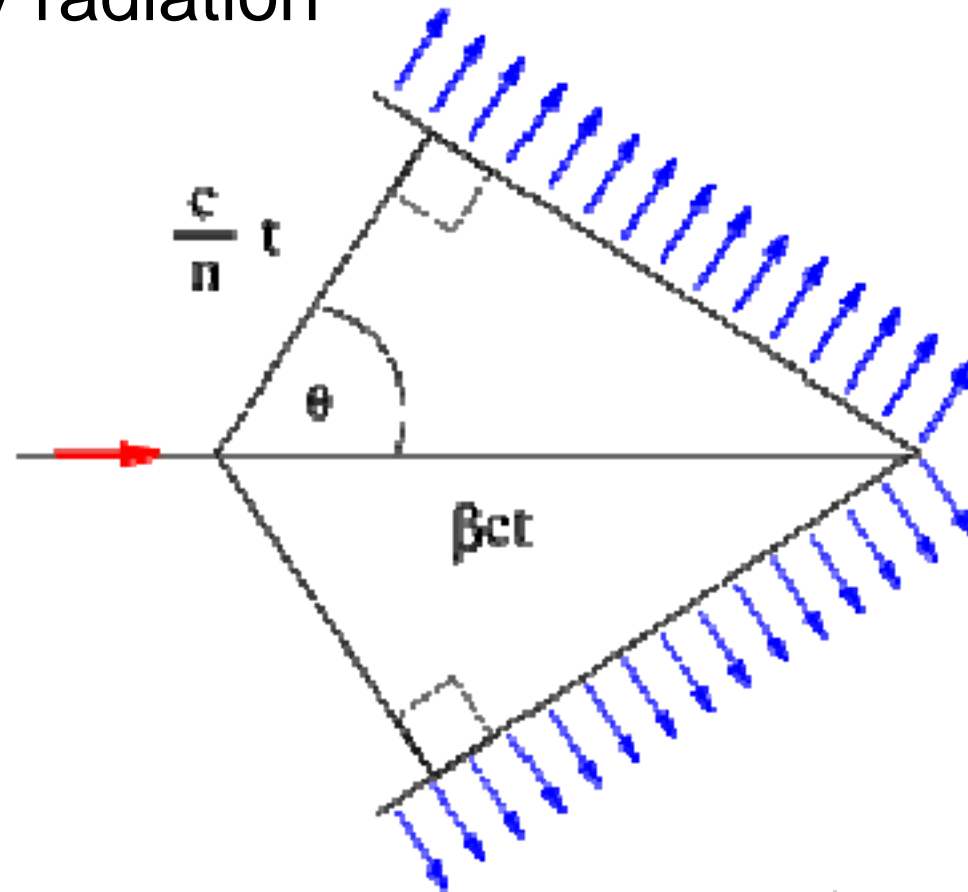
Non-linear THz spectroscopy

State of the art of the THz pulse power using fs laser

	Pump power		THz power		
		/pulse	average	/pulse	Electric field (V/cm)
Ti: Al ₂ O ₃ laser					
Amplifier@1KHz	650 mW	650 μJ	0.1μW	125 pJ	1 KV/cm
Oscillator with magnetic field (Sarukura 1.7T, @80MHz)	1500 mW 650 mW	18.75 nJ 8.125 nJ	650 μW 110 μW	8.125pJ 1.375pJ	0.25 KV/cm 0.1 KV/cm

Non-linear THz spectroscopy

- Cherenkov radiation



Cherenkov angle

$$\cos \theta = \frac{1}{n\beta}$$

Non-linear THz spectroscopy

- Basic idea of velocity matching by pulse front using Cherenkov effect with non-linear crystal

A. G. Stepanov, J. Hebling and J. Kuhl *et al.*, Appl. Phys. Lett. 83, 3000 (2003).

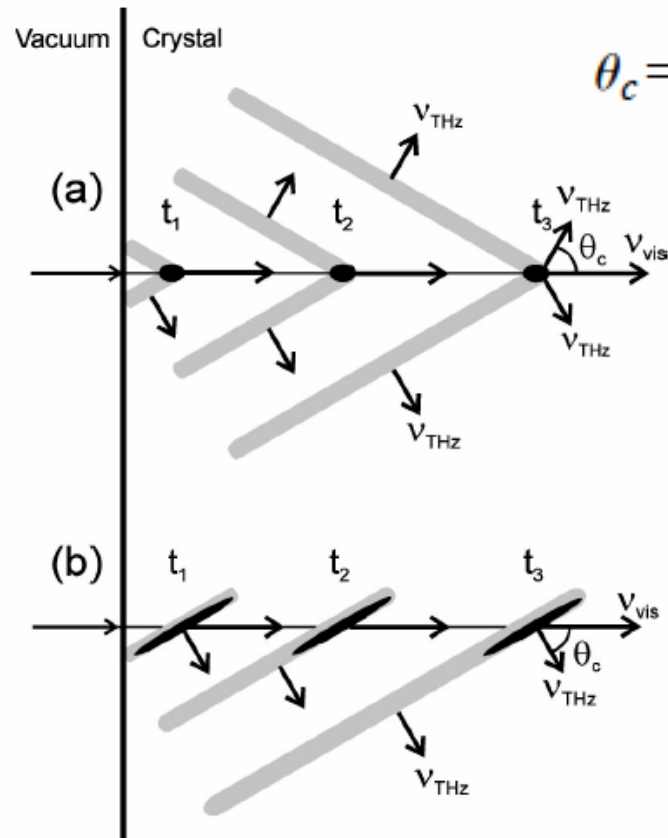


FIG. 1. Schematic illustration of the THz generation by tightly focused (a) and front tilted (b) femtosecond laser pulses propagating in an electro-optical crystal. Black ellipses and gray areas depict laser and generated THz pulses, respectively, at three different instants of time ($t_1 < t_2 < t_3$).

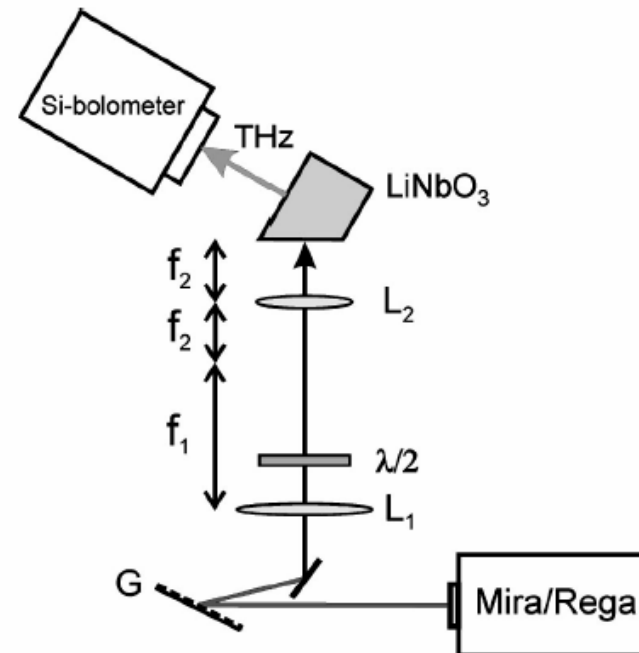
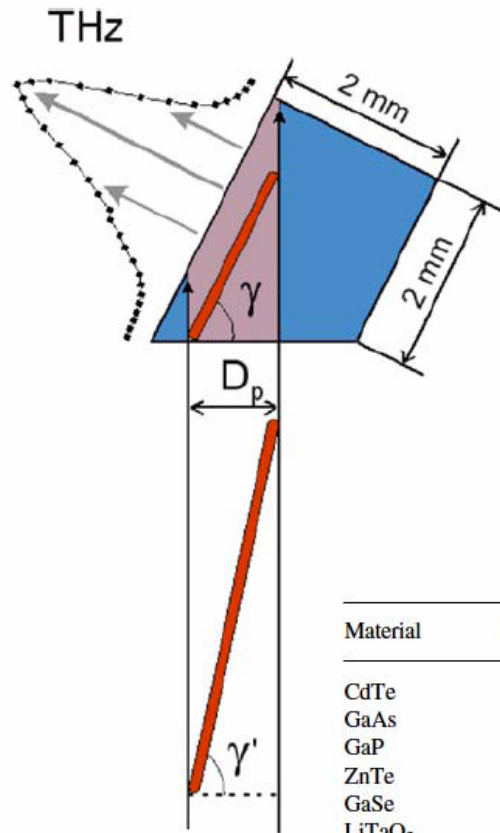


FIG. 2. Experimental setup used for the THz generation by femtosecond laser pulses with tilted pulse fronts.

Non-linear THz spectroscopy

- High power single cycle THz generation using tilted femtosecond light sources

J. Hebling and J. Kuhl *et al.*, Appl. Phys. B 78, 593-599 (2004).



$$v_{vis}^{gr} \cdot \cos \gamma = v_{THz}^{ph}$$

$$v_{vis}^{gr} \gg v_{THz}^{ph}$$

$$n_v^{gr} \ll n_{THz}$$

Material	r (pm/V)	d (pm/V)	n_v^*	n_v^{gr}	n_{THz}	α_{THz} (cm ⁻¹)	FOM (pm ² /V ²)	FOM _A (pm ² cm ² /V ²)
CdTe	4.5 ²⁶	81.8	2.92 ²⁴	3.73	3.23 ²⁰	4.8 ²⁰	242	10.5
GaAs	1.43 ²⁶	65.6	3.68 ¹⁸	4.18	3.61	0.5 ¹⁸	87.9	352
GaP	0.97 ²²	24.8	3.18 ¹⁸	3.57	3.34 ¹⁸	1.9 ¹⁸	18.2	5.0
ZnTe	4.04 ²⁶	68.5	2.87 ¹⁹	3.31	3.17 ²⁰	1.3 ²⁰	180	106
GaSe	1.7 ¹⁵	28.0	2.85 ¹⁷	3.13	3.72 ¹⁶	0.07 ¹⁸	25.9	5300
LiTaO ₃	30.5 ²⁶	161	2.145 ²⁵	2.22	6.42 ²¹	46 ²¹	882	0.4
LiNbO ₃	30.9 ²⁶	168	2.159 ²³	2.23	5.16 ²¹	10 ²¹		

Non-linear THz spectroscopy

- High power single cycle THz generation using tilted femtosecond light sources : Recent status

A. G. Stepanov and J. Heebing *et al.*, Optics Express 13 5762 (2005).

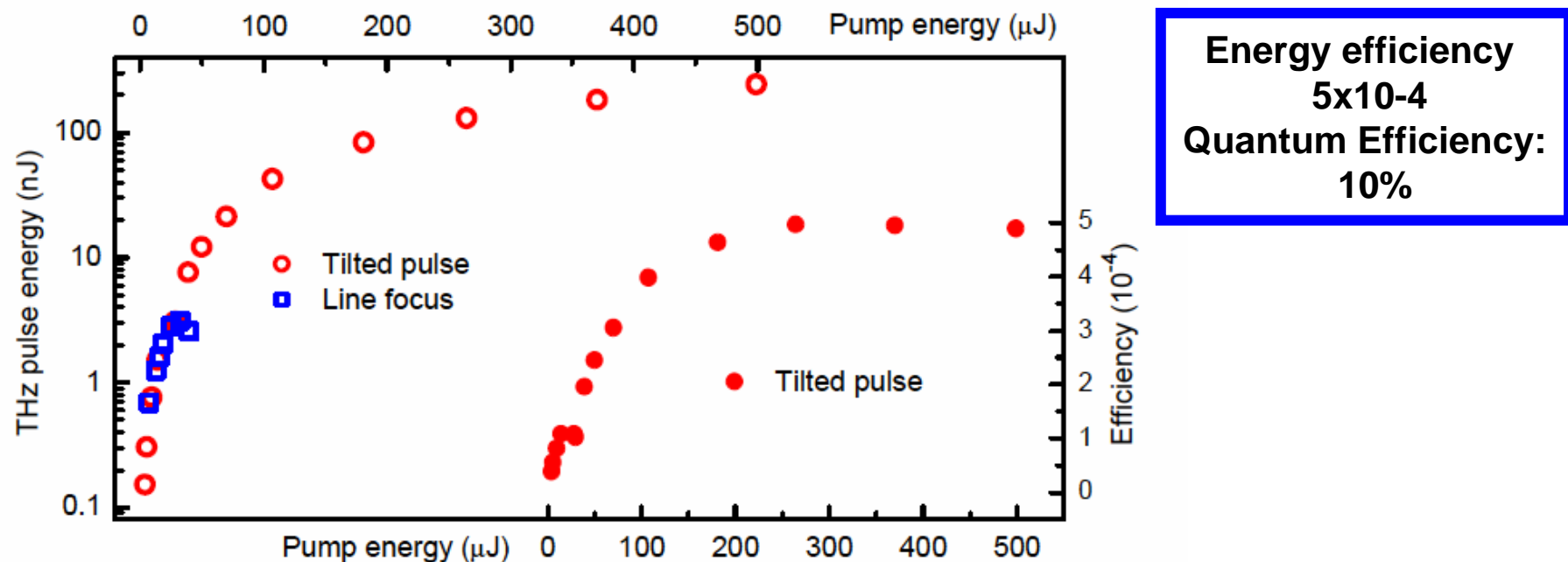


Fig. 1. Measured energy of THz pulses generated by the tilted pulse front (red circles) and line focusing (open blue squares) set-ups versus the energy of the 780 nm pump laser pulses (upper left part). Energy conversion efficiency versus the pump energy for the tilted pulse front set-up (lower right part).

$$P_{\text{THz}} = 100 \text{ nJ/pulse}, 10 \text{ nJ/cm}^2, 10 \text{ MW/cm}^2, |E_{\text{THz}}| \sim 30 \text{ kV/cm} = 3 \text{ MV/m}$$